

Mathematica 11.3 Integration Test Results

Test results for the 453 problems in "7.2.4a (f x)^m (d-c^2 d x^2)^p (a+b arccosh(c x))^n.m"

Problem 33: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcCosh}[c x]}{x (d - c^2 d x^2)} dx$$

Optimal (type 4, 61 leaves, 7 steps):

$$\frac{2 (a + b \operatorname{ArcCosh}[c x]) \operatorname{ArcTanh}\left[e^{2 \operatorname{ArcCosh}[c x]}\right]}{d} + \frac{b \operatorname{PolyLog}\left[2, -e^{2 \operatorname{ArcCosh}[c x]}\right]}{2 d} - \frac{b \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[c x]}\right]}{2 d}$$

Result (type 4, 124 leaves):

$$-\frac{1}{2 d} \left(-2 b \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + e^{-2 \operatorname{ArcCosh}[c x]}\right] + 2 b \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - e^{-\operatorname{ArcCosh}[c x]}\right] + 2 b \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + e^{-\operatorname{ArcCosh}[c x]}\right] - 2 a \operatorname{Log}[x] + a \operatorname{Log}\left[1 - c^2 x^2\right] + b \operatorname{PolyLog}\left[2, -e^{-2 \operatorname{ArcCosh}[c x]}\right] - 2 b \operatorname{PolyLog}\left[2, -e^{-\operatorname{ArcCosh}[c x]}\right] - 2 b \operatorname{PolyLog}\left[2, e^{-\operatorname{ArcCosh}[c x]}\right] \right)$$

Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{a + b \operatorname{ArcCosh}[c x]}{x (d - c^2 d x^2)^2} dx$$

Optimal (type 4, 116 leaves, 9 steps):

$$-\frac{b c x}{2 d^2 \sqrt{-1 + c x} \sqrt{1 + c x}} + \frac{a + b \operatorname{ArcCosh}[c x]}{2 d^2 (1 - c^2 x^2)} + \frac{2 (a + b \operatorname{ArcCosh}[c x]) \operatorname{ArcTanh}\left[e^{2 \operatorname{ArcCosh}[c x]}\right]}{d^2} + \frac{b \operatorname{PolyLog}\left[2, -e^{2 \operatorname{ArcCosh}[c x]}\right]}{2 d^2} - \frac{b \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[c x]}\right]}{2 d^2}$$

Result (type 4, 243 leaves):

$$\frac{1}{4d^2} \left(-b \sqrt{\frac{-1+cx}{1+cx}} + \frac{b \sqrt{\frac{-1+cx}{1+cx}}}{1-cx} + \frac{bcx \sqrt{\frac{-1+cx}{1+cx}}}{1-cx} - \frac{2a}{-1+c^2x^2} + \frac{b \operatorname{ArcCosh}[cx]}{1-cx} + \frac{b \operatorname{ArcCosh}[cx]}{1+cx} + \right.$$

$$4b \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 + e^{-2 \operatorname{ArcCosh}[cx]}\right] - 4b \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 - e^{-\operatorname{ArcCosh}[cx]}\right] -$$

$$4b \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 + e^{-\operatorname{ArcCosh}[cx]}\right] + 4a \operatorname{Log}[x] - 2a \operatorname{Log}\left[1 - c^2x^2\right] -$$

$$\left. 2b \operatorname{PolyLog}\left[2, -e^{-2 \operatorname{ArcCosh}[cx]}\right] + 4b \operatorname{PolyLog}\left[2, -e^{-\operatorname{ArcCosh}[cx]}\right] + 4b \operatorname{PolyLog}\left[2, e^{-\operatorname{ArcCosh}[cx]}\right] \right)$$

Problem 118: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{(d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 84 leaves, 3 steps):

$$\frac{x (a + b \operatorname{ArcCosh}[cx])}{d \sqrt{d - c^2 d x^2}} - \frac{b \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1 - c^2 x^2]}{2 c d \sqrt{d - c^2 d x^2}}$$

Result (type 8, 26 leaves):

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{(d - c^2 d x^2)^{3/2}} dx$$

Problem 120: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{x^2 (d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$-\frac{a + b \operatorname{ArcCosh}[cx]}{d x \sqrt{d - c^2 d x^2}} + \frac{2 c^2 x (a + b \operatorname{ArcCosh}[cx])}{d \sqrt{d - c^2 d x^2}} -$$

$$\frac{b c \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[x]}{d \sqrt{d - c^2 d x^2}} - \frac{b c \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1 - c^2 x^2]}{2 d \sqrt{d - c^2 d x^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{x^2 (d - c^2 d x^2)^{3/2}} dx$$

Problem 122: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{x^4 (d - c^2 d x^2)^{3/2}} dx$$

Optimal (type 3, 250 leaves, 6 steps):

$$\frac{bc \sqrt{-1+cx} \sqrt{1+cx}}{6dx^2 \sqrt{d-c^2dx^2}} - \frac{a+b \operatorname{ArcCosh}[cx]}{3dx^3 \sqrt{d-c^2dx^2}} - \frac{4c^2(a+b \operatorname{ArcCosh}[cx])}{3dx \sqrt{d-c^2dx^2}} + \frac{8c^4x(a+b \operatorname{ArcCosh}[cx])}{3d \sqrt{d-c^2dx^2}} - \frac{5bc^3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[x]}{3d \sqrt{d-c^2dx^2}} - \frac{bc^3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1-c^2x^2]}{2d \sqrt{d-c^2dx^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{x^4 (d - c^2 d x^2)^{3/2}} dx$$

Problem 127: Unable to integrate problem.

$$\int \frac{x^2 (a + b \operatorname{ArcCosh}[cx])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 160 leaves, 5 steps):

$$\frac{b \sqrt{-1+cx} \sqrt{1+cx}}{6c^3 d^2 (1-c^2x^2) \sqrt{d-c^2dx^2}} + \frac{x^3 (a + b \operatorname{ArcCosh}[cx])}{3d^2 (1-cx)(1+cx) \sqrt{d-c^2dx^2}} + \frac{b \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1-c^2x^2]}{6c^3 d^2 \sqrt{d-c^2dx^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{x^2 (a + b \operatorname{ArcCosh}[cx])}{(d - c^2 d x^2)^{5/2}} dx$$

Problem 129: Unable to integrate problem.

$$\int \frac{a + b \operatorname{ArcCosh}[cx]}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 189 leaves, 5 steps):

$$\frac{b \sqrt{-1+cx} \sqrt{1+cx}}{6 c d^2 (1-c^2 x^2) \sqrt{d-c^2 d x^2}} + \frac{2 x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 \sqrt{d-c^2 d x^2}} +$$

$$\frac{x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} - \frac{b \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1-c^2 x^2]}{3 c d^2 \sqrt{d-c^2 d x^2}}$$

Result (type 8, 26 leaves):

$$\int \frac{a+b \operatorname{ArcCosh}[c x]}{(d-c^2 d x^2)^{5/2}} dx$$

Problem 131: Unable to integrate problem.

$$\int \frac{a+b \operatorname{ArcCosh}[c x]}{x^2 (d-c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 279 leaves, 6 steps):

$$\frac{b c \sqrt{-1+cx} \sqrt{1+cx}}{6 d^2 (1-c^2 x^2) \sqrt{d-c^2 d x^2}} + \frac{8 c^2 x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 \sqrt{d-c^2 d x^2}} -$$

$$\frac{a+b \operatorname{ArcCosh}[c x]}{d^2 x (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} + \frac{4 c^2 x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} -$$

$$\frac{b c \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[x]}{d^2 \sqrt{d-c^2 d x^2}} - \frac{5 b c \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1-c^2 x^2]}{6 d^2 \sqrt{d-c^2 d x^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{a+b \operatorname{ArcCosh}[c x]}{x^2 (d-c^2 d x^2)^{5/2}} dx$$

Problem 133: Unable to integrate problem.

$$\int \frac{a+b \operatorname{ArcCosh}[c x]}{x^4 (d-c^2 d x^2)^{5/2}} dx$$

Optimal (type 3, 383 leaves, 6 steps):

$$\frac{b c \sqrt{-1+cx} \sqrt{1+cx}}{6 d^2 x^2 \sqrt{d-c^2 d x^2}} + \frac{b c^3 \sqrt{-1+cx} \sqrt{1+cx}}{6 d^2 (1-c^2 x^2) \sqrt{d-c^2 d x^2}} +$$

$$\frac{16 c^4 x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 \sqrt{d-c^2 d x^2}} - \frac{a+b \operatorname{ArcCosh}[c x]}{3 d^2 x^3 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} -$$

$$\frac{2 c^2 (a+b \operatorname{ArcCosh}[c x])}{d^2 x (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} + \frac{8 c^4 x (a+b \operatorname{ArcCosh}[c x])}{3 d^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} -$$

$$\frac{8 b c^3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[x]}{3 d^2 \sqrt{d-c^2 d x^2}} - \frac{4 b c^3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{Log}[1-c^2 x^2]}{3 d^2 \sqrt{d-c^2 d x^2}}$$

Result (type 8, 29 leaves):

$$\int \frac{a + b \operatorname{ArcCosh}[c x]}{x^4 (d - c^2 d x^2)^{5/2}} dx$$

Problem 143: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{(f x)^{3/2} (a + b \operatorname{ArcCosh}[c x])}{\sqrt{1 - c^2 x^2}} dx$$

Optimal (type 5, 111 leaves, 2 steps):

$$\frac{2 (f x)^{5/2} (a + b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2 x^2\right]}{5 f} + \frac{1}{35 f^2 \sqrt{1 - c^2 x^2}}$$

$$4 b c (f x)^{7/2} \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, c^2 x^2\right]$$

Result (type 5, 230 leaves):

$$\frac{1}{36 c^2 \sqrt{1 - c^2 x^2}} f \sqrt{f x} \left(\frac{24 i a \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}\right], -1\right]}{\sqrt{-\frac{1}{c}}} + \right.$$

$$8 (1 + c x) \left(-3 a + 3 a c x - 2 b c x \sqrt{\frac{-1 + c x}{1 + c x}} + 3 b (-1 + c x) \operatorname{ArcCosh}[c x] - \right.$$

$$\left. \left. 3 b (-1 + c x) \operatorname{ArcCosh}[c x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right] \right) + \right.$$

$$\left. \left(3 \sqrt{2} b c \pi x \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2 x^2\right] \right) / \right.$$

$$\left. \left(\Gamma\left[\frac{5}{4}\right] \Gamma\left[\frac{7}{4}\right] \right) \right)$$

Problem 144: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{(f x)^{3/2} (a + b \operatorname{ArcCosh}[c x])}{\sqrt{d - c^2 d x^2}} dx$$

Optimal (type 5, 141 leaves, 2 steps):

$$\frac{1}{5 f \sqrt{d - c^2 d x^2}} 2 (f x)^{5/2} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{5}{4}, \frac{9}{4}, c^2 x^2\right] + \left(4 b c (f x)^{7/2} \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{HypergeometricPFQ}\left[\left\{1, \frac{7}{4}, \frac{7}{4}\right\}, \left\{\frac{9}{4}, \frac{11}{4}\right\}, c^2 x^2\right]\right) / \left(35 f^2 \sqrt{d - c^2 d x^2}\right)$$

Result (type 5, 241 leaves):

$$\frac{1}{36 c^2 \sqrt{d - c^2 d x^2} \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right]} f \sqrt{f x} \left(8 \operatorname{Gamma}\left[\frac{5}{4}\right] \operatorname{Gamma}\left[\frac{7}{4}\right] \left(\frac{3 i a \sqrt{1 - \frac{1}{c^2 x^2}} \sqrt{x} \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{-\frac{1}{c}}}{\sqrt{x}}\right], -1\right]}{\sqrt{-\frac{1}{c}}} + (1 + c x) \left(-3 a + 3 a c x - 2 b c x \sqrt{\frac{-1 + c x}{1 + c x}} + 3 b (-1 + c x) \operatorname{ArcCosh}[c x] - 3 b (-1 + c x) \operatorname{ArcCosh}[c x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{5}{4}, c^2 x^2\right] \right) \right) + 3 \sqrt{2} b c \pi x \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \operatorname{HypergeometricPFQ}\left[\left\{\frac{3}{4}, \frac{3}{4}, 1\right\}, \left\{\frac{5}{4}, \frac{7}{4}\right\}, c^2 x^2\right] \right)$$

Problem 145: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x^m (d - c^2 d x^2)^3 (a + b \operatorname{ArcCosh}[c x]) dx$$

Optimal (type 5, 389 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{b c d^3 (2271 + 1329 m + 284 m^2 + 27 m^3 + m^4) x^{2+m} (1 - c^2 x^2)}{(3+m)^2 (5+m)^2 (7+m)^2 \sqrt{-1+cx} \sqrt{1+cx}} + \\
 & \frac{b c^3 d^3 (9+m) (13+2m) x^{4+m} (1 - c^2 x^2)}{(5+m)^2 (7+m)^2 \sqrt{-1+cx} \sqrt{1+cx}} - \frac{b c^5 d^3 x^{6+m} (1 - c^2 x^2)}{(7+m)^2 \sqrt{-1+cx} \sqrt{1+cx}} + \\
 & \frac{d^3 x^{1+m} (a + b \operatorname{ArcCosh}[cx])}{1+m} - \frac{3 c^2 d^3 x^{3+m} (a + b \operatorname{ArcCosh}[cx])}{3+m} + \frac{3 c^4 d^3 x^{5+m} (a + b \operatorname{ArcCosh}[cx])}{5+m} - \\
 & \frac{c^6 d^3 x^{7+m} (a + b \operatorname{ArcCosh}[cx])}{7+m} - \left(3 b c d^3 (2161 + 1813 m + 455 m^2 + 35 m^3) \right. \\
 & \quad \left. x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right] \right) / \\
 & \left((1+m) (2+m) (3+m)^2 (5+m)^2 (7+m)^2 \sqrt{-1+cx} \sqrt{1+cx} \right)
 \end{aligned}$$

Result (type 6, 3418 leaves):

$$\begin{aligned}
 & \frac{a d^3 x^{1+m}}{1+m} - \frac{3 a c^2 d^3 x^{3+m}}{3+m} + \frac{3 a c^4 d^3 x^{5+m}}{5+m} - \frac{a c^6 d^3 x^{7+m}}{7+m} + \frac{1}{c} b d^3 x^m (cx)^{-m} \\
 & \left(- \frac{1}{1+m} 12 (cx)^m \left(\left(\sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) / \right. \right. \\
 & \quad \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] + (-1+cx) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) \right) \left. \right) - \\
 & \left(\sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] + (-1+cx) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) \right) \left. \right) + \\
 & \left. \frac{(cx)^{1+m} \operatorname{ArcCosh}[cx]}{1+m} \right) - 3 b c d^3 x^{2+m} (cx)^{-2-m} \left(- \frac{1}{3+m} 4 (cx)^m \right. \\
 & \left(\left(3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) / \right. \\
 & \quad \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx)\right] + (-1+cx) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \right. \right. \right. \\
 & \quad \quad \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx)\right] \right) \right) \left. \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 \sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & (-1+cx)^{3/2} \sqrt{1+cx} \left(\left(5 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \right. \\
 & \left. \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & \left(7(-1+cx) \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(70 \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 5(-1+cx) \right. \\
 & \left. \left(4m \operatorname{AppellF1}\left[\frac{7}{2}, 1-m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, \right. \right. \right. \\
 & \left. \left. \left. 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) + \frac{(cx)^{3+m} \operatorname{ArcCosh}[cx]}{3+m} + 3bc^3 d^3 x^{4+m} (cx)^{-4-m} \\
 & \left(-\frac{1}{5+m} \left(\left(12 (cx)^m \sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \right. \\
 & \left. \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) - \\
 & \left(12 (cx)^m \sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & 4m(-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \\
 & \left. (-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) + \\
 & \left(40 (cx)^m (-1+cx)^{3/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx) \right] + \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) + \\
 & \left(112 (cx)^m (-1+cx)^{5/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(70 \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 5(-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{7}{2}, 1-m, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx) \right] + \operatorname{AppellF1}\left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) + \\
 & \left(108 (cx)^m (-1+cx)^{7/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(7 \left(18 \operatorname{AppellF1}\left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \left. \left. (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{9}{2}, 1-m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{9}{2}, -m, \frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) \right) + \\
 & \left(44 (cx)^m (-1+cx)^{9/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(9 \left(22 \operatorname{AppellF1}\left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \right. \right. \\
 & \left. \left. \left(4m \operatorname{AppellF1}\left[\frac{11}{2}, 1-m, -\frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{11}{2}, -m, \frac{1}{2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) \right) + \frac{(cx)^{5+m} \operatorname{ArcCosh}[cx]}{5+m} \Bigg) - b c^5 d^3 x^{6+m} (cx)^{-6-m} \\
 & \left(-\frac{1}{7+m} \left(\left(12 (cx)^m \sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \right. \\
 & \left. \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \right. \right. \right. \\
 & \left. \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) - \\
 & \left(12 (cx)^m \sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \left. 4m(-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \right. \\
 & \left. (-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) + \\
 & \left(60 (cx)^m (-1+cx)^{3/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)] + \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \Big) \Big) + \\
 & \left(252 (cx)^m (-1+cx)^{5/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(70 \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 5(-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{7}{2}, 1-m, \right. \right. \right. \\
 & \quad \left. \left. -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \Big) \Big) + \\
 & \left(468 (cx)^m (-1+cx)^{7/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(7 \left(18 \operatorname{AppellF1}\left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \quad (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{9}{2}, 1-m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{9}{2}, -m, \frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \Big) \Big) + \\
 & \left(484 (cx)^m (-1+cx)^{9/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(9 \left(22 \operatorname{AppellF1}\left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \quad (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{11}{2}, 1-m, -\frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{11}{2}, -m, \frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \Big) \Big) + \\
 & \left(260 (cx)^m (-1+cx)^{11/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{11}{2}, -m, -\frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(11 \left(26 \operatorname{AppellF1}\left[\frac{11}{2}, -m, -\frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \quad (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{13}{2}, 1-m, -\frac{1}{2}, \frac{15}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{13}{2}, -m, \frac{1}{2}, \frac{15}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \Big) \Big) + \\
 & \left(60 (cx)^m (-1+cx)^{13/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{13}{2}, -m, -\frac{1}{2}, \frac{15}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(13 \left(30 \operatorname{AppellF1}\left[\frac{13}{2}, -m, -\frac{1}{2}, \frac{15}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \quad (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{15}{2}, 1-m, -\frac{1}{2}, \frac{17}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \quad \left. \left. \operatorname{AppellF1}\left[\frac{15}{2}, -m, \frac{1}{2}, \frac{17}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \Big) \Big) + \frac{(cx)^{7+m} \operatorname{ArcCosh}[cx]}{7+m} \Big)
 \end{aligned}$$

Problem 146: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x^m (d - c^2 d x^2)^2 (a + b \operatorname{ArcCosh}[c x]) dx$$

Optimal (type 5, 277 leaves, 7 steps):

$$\begin{aligned} & -\frac{b c d^2 (38 + 13 m + m^2) x^{2+m} (1 - c^2 x^2)}{(3 + m)^2 (5 + m)^2 \sqrt{-1 + c x} \sqrt{1 + c x}} + \frac{b c^3 d^2 x^{4+m} (1 - c^2 x^2)}{(5 + m)^2 \sqrt{-1 + c x} \sqrt{1 + c x}} + \\ & \frac{d^2 x^{1+m} (a + b \operatorname{ArcCosh}[c x])}{1 + m} - \frac{2 c^2 d^2 x^{3+m} (a + b \operatorname{ArcCosh}[c x])}{3 + m} + \frac{c^4 d^2 x^{5+m} (a + b \operatorname{ArcCosh}[c x])}{5 + m} - \\ & \left(\frac{b c d^2 (149 + 100 m + 15 m^2) x^{2+m} \sqrt{1 - c^2 x^2} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{\left((1 + m)(2 + m)(3 + m)^2 (5 + m)^2 \sqrt{-1 + c x} \sqrt{1 + c x}\right)} \right) / \end{aligned}$$

Result (type 6, 2070 leaves):

$$\begin{aligned} & \frac{a d^2 x^{1+m}}{1 + m} - \frac{2 a c^2 d^2 x^{3+m}}{3 + m} + \frac{a c^4 d^2 x^{5+m}}{5 + m} + \frac{1}{c} b d^2 x^m (c x)^{-m} \\ & \left(-\frac{1}{1 + m} 12 (c x)^m \left(\left(\sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) / \right. \right. \\ & \quad \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] + (-1 + c x) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1 - m, \right. \right. \right. \\ & \quad \left. \left. \left. -\frac{1}{2}, \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) \right) \right) - \\ & \quad \left(\sqrt{\frac{-1 + c x}{1 + c x}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) / \\ & \quad \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] + (-1 + c x) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1 - m, \frac{1}{2}, \right. \right. \right. \\ & \quad \left. \left. \left. \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) \right) \right) + \\ & \left. \frac{(c x)^{1+m} \operatorname{ArcCosh}[c x]}{1 + m} \right) - 2 b c d^2 x^{2+m} (c x)^{-2-m} \left(-\frac{1}{3 + m} 4 (c x)^m \right. \\ & \left(3 \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) / \\ & \quad \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] + (-1 + c x) \left(4 m \operatorname{AppellF1}\left[\frac{3}{2}, 1 - m, \right. \right. \right. \\ & \quad \left. \left. \left. -\frac{1}{2}, \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) \right) \right) - \\ & \quad \left(3 \sqrt{\frac{-1 + c x}{1 + c x}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1 - c x, \frac{1}{2} (1 - c x)\right] \right) / \end{aligned}$$

$$\begin{aligned}
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & (-1+cx)^{3/2} \sqrt{1+cx} \left(\left(5 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \right. \\
 & \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & \left(7(-1+cx) \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(70 \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 5(-1+cx) \right. \\
 & \left(4m \operatorname{AppellF1}\left[\frac{7}{2}, 1-m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, \right. \right. \\
 & \left. \left. 1-cx, \frac{1}{2}(1-cx)\right] \right) \left. \right) + \frac{(cx)^{3+m} \operatorname{ArcCosh}[cx]}{3+m} + bc^3 d^2 x^{4+m} (cx)^{-4-m} \\
 & \left(-\frac{1}{5+m} \left(\left(12 (cx)^m \sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \right. \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \right. \right. \right. \\
 & \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) - \\
 & \left(12 (cx)^m \sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \\
 & 4m(-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \\
 & \left. (-1+cx) \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) + \\
 & \left(40 (cx)^m (-1+cx)^{3/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, \right. \right. \right. \\
 & \left. \left. -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & \left(112 (cx)^m (-1+cx)^{5/2} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(70 \operatorname{AppellF1} \left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + 5 (-1+cx) \left(4m \operatorname{AppellF1} \left[\frac{7}{2}, 1-m, \right. \right. \right. \\
 & \quad \left. \left. \left. -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \operatorname{AppellF1} \left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) \right) + \\
 & \left(108 (cx)^m (-1+cx)^{7/2} \sqrt{1+cx} \operatorname{AppellF1} \left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) / \\
 & \left(7 \left(18 \operatorname{AppellF1} \left[\frac{7}{2}, -m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \right. \right. \\
 & \quad \left. \left. (-1+cx) \left(4m \operatorname{AppellF1} \left[\frac{9}{2}, 1-m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[\frac{9}{2}, -m, \frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) \right) \right) + \\
 & \left(44 (cx)^m (-1+cx)^{9/2} \sqrt{1+cx} \operatorname{AppellF1} \left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) / \\
 & \left(9 \left(22 \operatorname{AppellF1} \left[\frac{9}{2}, -m, -\frac{1}{2}, \frac{11}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \right. \right. \\
 & \quad \left. \left. (-1+cx) \left(4m \operatorname{AppellF1} \left[\frac{11}{2}, 1-m, -\frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{AppellF1} \left[\frac{11}{2}, -m, \frac{1}{2}, \frac{13}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) \right) \right) \right) + \frac{(cx)^{5+m} \operatorname{ArcCosh}[cx]}{5+m}
 \end{aligned}$$

Problem 147: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int x^m (d - c^2 dx^2) (a + b \operatorname{ArcCosh}[cx]) dx$$

Optimal (type 5, 164 leaves, 6 steps):

$$\frac{bcdx^{2+m} \sqrt{-1+cx} \sqrt{1+cx}}{(3+m)^2} + \frac{dx^{1+m} (a + b \operatorname{ArcCosh}[cx])}{1+m} - \frac{c^2 dx^{3+m} (a + b \operatorname{ArcCosh}[cx])}{3+m} - \\
 \frac{bcd(7+3m)x^{2+m} \sqrt{1-c^2x^2} \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, \frac{2+m}{2}, \frac{4+m}{2}, c^2x^2 \right]}{(1+m)(2+m)(3+m)^2 \sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 6, 1038 leaves):

$$\frac{adx^{1+m}}{1+m} - \frac{ac^2dx^{3+m}}{3+m} + \frac{1}{c} bdx^m (cx)^{-m} \\
 \left(-\frac{1}{1+m} 12 (cx)^m \left(\left(\sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1} \left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) / \right. \right. \\
 \left. \left. \left(6 \operatorname{AppellF1} \left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + (-1+cx) \left(4m \operatorname{AppellF1} \left[\frac{3}{2}, 1-m, \right. \right. \right. \right. \right. \\
 \left. \left. \left. \left. -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx) \right] + \operatorname{AppellF1} \left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2} (1-cx) \right] \right) \right) \right) \right) -$$

$$\begin{aligned}
 & \left(\sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & \left. \frac{(cx)^{1+m} \operatorname{ArcCosh}[cx]}{1+m} \right) - bcdx^{2+m}(cx)^{-2-m} \left(-\frac{1}{3+m} 4(cx)^m \right. \\
 & \left. \left(\left(3 \sqrt{-1+cx} \sqrt{1+cx} \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \right. \\
 & \left. \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, -\frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) - \\
 & \left(3 \sqrt{\frac{-1+cx}{1+cx}} \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \\
 & \left(6 \operatorname{AppellF1}\left[\frac{1}{2}, -m, \frac{1}{2}, \frac{3}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{3}{2}, 1-m, \frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] - \operatorname{AppellF1}\left[\frac{3}{2}, -m, \frac{3}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \\
 & (-1+cx)^{3/2} \sqrt{1+cx} \left(\left(5 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \right. \\
 & \left(30 \operatorname{AppellF1}\left[\frac{3}{2}, -m, -\frac{1}{2}, \frac{5}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 3(-1+cx) \right. \\
 & \left. \left(4m \operatorname{AppellF1}\left[\frac{5}{2}, 1-m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, -m, \frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) + \left(7(-1+cx) \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) / \left(70 \operatorname{AppellF1}\left[\frac{5}{2}, -m, -\frac{1}{2}, \frac{7}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + 5 \right. \\
 & \left. (-1+cx) \left(4m \operatorname{AppellF1}\left[\frac{7}{2}, 1-m, -\frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] + \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{7}{2}, -m, \frac{1}{2}, \frac{9}{2}, 1-cx, \frac{1}{2}(1-cx)\right] \right) \right) \right) + \frac{(cx)^{3+m} \operatorname{ArcCosh}[cx]}{3+m} \Bigg)
 \end{aligned}$$

Problem 151: Unable to integrate problem.

$$\int x^m (d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcCosh}[c x]) dx$$

Optimal (type 5, 709 leaves, 10 steps):

$$\begin{aligned} & - \frac{15 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(2+m)^2 (4+m) (6+m) \sqrt{-1+c x} \sqrt{1+c x}} - \\ & \frac{5 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(6+m) (8+6m+m^2) \sqrt{-1+c x} \sqrt{1+c x}} - \frac{b c d^2 x^{2+m} \sqrt{d - c^2 d x^2}}{(12+8m+m^2) \sqrt{-1+c x} \sqrt{1+c x}} + \\ & \frac{5 b c^3 d^2 x^{4+m} \sqrt{d - c^2 d x^2}}{(4+m)^2 (6+m) \sqrt{-1+c x} \sqrt{1+c x}} + \frac{2 b c^3 d^2 x^{4+m} \sqrt{d - c^2 d x^2}}{(4+m) (6+m) \sqrt{-1+c x} \sqrt{1+c x}} - \\ & \frac{b c^5 d^2 x^{6+m} \sqrt{d - c^2 d x^2}}{(6+m)^2 \sqrt{-1+c x} \sqrt{1+c x}} + \frac{15 d^2 x^{1+m} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])}{(6+m) (8+6m+m^2)} + \\ & \frac{5 d^2 x^{1+m} (1-c x) (1+c x) \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])}{(4+m) (6+m)} + \\ & \frac{d^2 x^{1+m} (1-c x)^2 (1+c x)^2 \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])}{6+m} + \\ & \left(15 d^2 x^{1+m} \sqrt{1-c^2 x^2} \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x]) \right. \\ & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) / \left((6+m) (8+14m+7m^2+m^3) (1-c x) (1+c x) \right) - \\ & \left(15 b c d^2 x^{2+m} \sqrt{d - c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right] \right) / \\ & \left((1+m) (2+m)^2 (4+m) (6+m) \sqrt{-1+c x} \sqrt{1+c x} \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m (d - c^2 d x^2)^{5/2} (a + b \operatorname{ArcCosh}[c x]) dx$$

Problem 152: Unable to integrate problem.

$$\int x^m (d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcCosh}[c x]) dx$$

Optimal (type 5, 442 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{3 b c d x^{2+m} \sqrt{d-c^2 d x^2}}{(2+m)^2 (4+m) \sqrt{-1+c x} \sqrt{1+c x}} - \frac{b c d x^{2+m} \sqrt{d-c^2 d x^2}}{(8+6 m+m^2) \sqrt{-1+c x} \sqrt{1+c x}} + \\
 & \frac{b c^3 d x^{4+m} \sqrt{d-c^2 d x^2}}{(4+m)^2 \sqrt{-1+c x} \sqrt{1+c x}} + \frac{3 d x^{1+m} \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{8+6 m+m^2} + \\
 & \frac{d x^{1+m} (1-c x) (1+c x) \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{4+m} + \\
 & \left(3 d x^{1+m} \sqrt{1-c^2 x^2} \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \right. \\
 & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]\right) / \left((8+14 m+7 m^2+m^3) (1-c x) (1+c x) \right) - \\
 & \left(3 b c d x^{2+m} \sqrt{d-c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right]\right) / \\
 & \left((1+m) (2+m)^2 (4+m) \sqrt{-1+c x} \sqrt{1+c x} \right)
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m (d-c^2 d x^2)^{3/2} (a+b \operatorname{ArcCosh}[c x]) dx$$

Problem 153: Unable to integrate problem.

$$\int x^m \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) dx$$

Optimal (type 5, 268 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{b c x^{2+m} \sqrt{d-c^2 d x^2}}{(2+m)^2 \sqrt{-1+c x} \sqrt{1+c x}} + \frac{x^{1+m} \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{2+m} + \\
 & \left(x^{1+m} \sqrt{1-c^2 x^2} \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right]\right) / \\
 & \left((2+3 m+m^2) (1-c x) (1+c x) \right) - \\
 & \left(b c x^{2+m} \sqrt{d-c^2 d x^2} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right]\right) / \\
 & \left((1+m) (2+m)^2 \sqrt{-1+c x} \sqrt{1+c x} \right)
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int x^m \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) dx$$

Problem 154: Unable to integrate problem.

$$\int \frac{x^m (a+b \operatorname{ArcCosh}[c x])}{\sqrt{d-c^2 d x^2}} dx$$

Optimal (type 5, 166 leaves, 2 steps):

$$\begin{aligned} & \left(x^{1+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) / \\ & \left((1+m) \sqrt{d-c^2 d x^2} \right) + \\ & \left(b c x^{2+m} \sqrt{-1+c x} \sqrt{1+c x} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right] \right) / \\ & \left((2+3 m+m^2) \sqrt{d-c^2 d x^2} \right) \end{aligned}$$

Result (type 9, 198 leaves):

$$\begin{aligned} & \left(2^{-2-m} x^{1+m} \left(2^{2+m} \left(a \sqrt{1-c^2 x^2} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] + \right. \right. \right. \\ & \quad \left. \left. b (1-c^2 x^2) \operatorname{ArcCosh}[c x] \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) + \right. \\ & \quad \left. b c (1+m) \sqrt{\pi} x \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{Gamma}[1+m] \operatorname{HypergeometricPFQRegularized}\left[\right. \right. \\ & \quad \left. \left. \left\{1, \frac{2+m}{2}, \frac{2+m}{2}\right\}, \left\{\frac{3+m}{2}, \frac{4+m}{2}\right\}, c^2 x^2\right] \right) \Bigg) / \left((1+m) \sqrt{d-c^2 d x^2} \right) \end{aligned}$$

Problem 155: Unable to integrate problem.

$$\int \frac{x^m (a+b \operatorname{ArcCosh}[c x])}{(d-c^2 d x^2)^{3/2}} dx$$

Optimal (type 5, 280 leaves, 4 steps):

$$\begin{aligned} & \frac{x^{1+m} (a+b \operatorname{ArcCosh}[c x])}{d \sqrt{d-c^2 d x^2}} - \\ & \left(m x^{1+m} \sqrt{1-c^2 x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) / \\ & \left(d (1+m) \sqrt{d-c^2 d x^2} \right) + \frac{b c x^{2+m} \sqrt{-1+c x} \sqrt{1+c x} \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{d (2+m) \sqrt{d-c^2 d x^2}} - \\ & \left(b c m x^{2+m} \sqrt{-1+c x} \sqrt{1+c x} \operatorname{HypergeometricPFQ}\left[\left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3}{2}+\frac{m}{2}, 2+\frac{m}{2}\right\}, c^2 x^2\right] \right) / \\ & \left(d (2+3 m+m^2) \sqrt{d-c^2 d x^2} \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{x^m (a+b \operatorname{ArcCosh}[c x])}{(d-c^2 d x^2)^{3/2}} dx$$

Problem 156: Unable to integrate problem.

$$\int \frac{x^m (a + b \operatorname{ArcCosh}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Optimal (type 5, 435 leaves, 6 steps):

$$\begin{aligned} & \frac{(2-m) x^{1+m} (a + b \operatorname{ArcCosh}[c x])}{3 d^2 \sqrt{d - c^2 d x^2}} + \frac{x^{1+m} (a + b \operatorname{ArcCosh}[c x])}{3 d^2 (1 - c x) (1 + c x) \sqrt{d - c^2 d x^2}} - \\ & \left((2-m) m x^{1+m} \sqrt{1 - c^2 x^2} (a + b \operatorname{ArcCosh}[c x]) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, c^2 x^2\right] \right) / \\ & \left(3 d^2 (1+m) \sqrt{d - c^2 d x^2} \right) + \\ & \left(b c (2-m) x^{2+m} \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right] \right) / \\ & \left(3 d^2 (2+m) \sqrt{d - c^2 d x^2} \right) + \frac{b c x^{2+m} \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{Hypergeometric2F1}\left[2, \frac{2+m}{2}, \frac{4+m}{2}, c^2 x^2\right]}{3 d^2 (2+m) \sqrt{d - c^2 d x^2}} - \\ & \left(b c (2-m) m x^{2+m} \sqrt{-1 + c x} \sqrt{1 + c x} \operatorname{HypergeometricPFQ}\left[\left\{1, 1 + \frac{m}{2}, 1 + \frac{m}{2}\right\}, \right. \right. \\ & \left. \left. \left\{\frac{3}{2} + \frac{m}{2}, 2 + \frac{m}{2}\right\}, c^2 x^2\right] \right) / \left(3 d^2 (2 + 3 m + m^2) \sqrt{d - c^2 d x^2} \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{x^m (a + b \operatorname{ArcCosh}[c x])}{(d - c^2 d x^2)^{5/2}} dx$$

Problem 157: Unable to integrate problem.

$$\int \frac{x^m \operatorname{ArcCosh}[a x]}{\sqrt{1 - a^2 x^2}} dx$$

Optimal (type 5, 131 leaves, 2 steps):

$$\begin{aligned} & \frac{x^{1+m} \operatorname{ArcCosh}[a x] \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+m}{2}, \frac{3+m}{2}, a^2 x^2\right]}{1+m} + \\ & \left(a x^{2+m} \sqrt{-1 + a x} \sqrt{1 + a x} \operatorname{HypergeometricPFQ}\left[\left\{1, 1 + \frac{m}{2}, 1 + \frac{m}{2}\right\}, \left\{\frac{3}{2} + \frac{m}{2}, 2 + \frac{m}{2}\right\}, a^2 x^2\right] \right) / \\ & \left((2 + 3 m + m^2) \sqrt{1 - a^2 x^2} \right) \end{aligned}$$

Result (type 9, 163 leaves):

$$\begin{aligned}
 & - \left(\left(x^{1+m} \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \right. \right. \\
 & \left. \left. \left(\frac{1}{1+m} 2 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \operatorname{ArcCosh}[ax] \operatorname{Hypergeometric2F1}\left[1, 1+\frac{m}{2}, \frac{3+m}{2}, a^2 x^2\right] - \right. \right. \right. \\
 & \left. \left. \left. 2^{-1-m} a \sqrt{\pi} x \operatorname{Gamma}[1+m] \operatorname{HypergeometricPFQRegularized}\left[\right. \right. \right. \\
 & \left. \left. \left. \left\{1, 1+\frac{m}{2}, 1+\frac{m}{2}\right\}, \left\{\frac{3+m}{2}, 2+\frac{m}{2}\right\}, a^2 x^2\right] \right) \right) \left. \right) / \left(2 \sqrt{-(-1+ax)(1+ax)} \right)
 \end{aligned}$$

Problem 170: Result more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2}{x^3} dx$$

Optimal (type 4, 427 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{b c \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{x \sqrt{-1+c x} \sqrt{1+c x}} - \frac{\sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2}{2 x^2} + \\
 & \frac{c^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\
 & \frac{b^2 c^2 \sqrt{d-c^2 d x^2} \operatorname{ArcTan}\left[\sqrt{-1+c x} \sqrt{1+c x}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\
 & \frac{i b c^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\
 & \frac{i b c^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\
 & \frac{i b^2 c^2 \sqrt{d-c^2 d x^2} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \frac{i b^2 c^2 \sqrt{d-c^2 d x^2} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}}
 \end{aligned}$$

Result (type 4, 5075 leaves):

$$\begin{aligned}
 & - \frac{a^2 \sqrt{-d(-1+c^2 x^2)}}{2 x^2} - \frac{1}{2} a^2 c^2 \sqrt{d} \operatorname{Log}[x] + \frac{1}{2} a^2 c^2 \sqrt{d} \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d(-1+c^2 x^2)}\right] + \\
 & \left(i a b c^2 d \left(- \frac{i \sqrt{\frac{-1+c x}{1+c x}} (1+c x)}{c x} - \frac{i (-1+c x) (1+c x) \operatorname{ArcCosh}[c x]}{c^2 x^2} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right] - \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \\
 & \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right] + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[cx]}\right] \right) \Bigg/ \left(\sqrt{-d(-1+cx)(1+cx)}\right) + \\
 & b^2 c^2 \left(\frac{d \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \left(2 + \frac{\sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx]}{cx}\right)}{2cx \sqrt{-d(-1+cx)(1+cx)}} + \right. \\
 & \frac{1}{2 \sqrt{-d(-1+cx)(1+cx)}} i d \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \left(4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + \right. \\
 & \operatorname{ArcCosh}[cx]^2 \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right] - \operatorname{ArcCosh}[cx]^2 \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1-i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] + \right. \\
 & \left. 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1+i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] + \right. \\
 & 2 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right]^2 \operatorname{Log}\left[\frac{1}{1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right]^2 \operatorname{Log}\left[-\frac{2}{-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]^2 - 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right]^2 \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + 2 \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \left. \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \right.
 \end{aligned}
 \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]^2 \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \right) \right]^2 \operatorname{Log} \left[\frac{(1 - i) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
 & 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
 & \operatorname{Log} \left[\frac{(1 - i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\frac{(1 - i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
 & 2 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
 & \operatorname{Log} \left[\frac{(1 - i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
 & 2 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \right) \right]^2 \operatorname{Log} \left[(1 - i) \left(i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \right) \right]^2 \operatorname{Log} \left[\frac{(1 + i) \left(i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - \\
 & 4 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \right) \right] \operatorname{Log} \left[\frac{1}{2} \left((1 + i) - (1 - i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
 & \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 4 \operatorname{Log} \left[\frac{1}{2} \left((1 + i) - (1 - i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
 & \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + 4 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1 + c x}{1 + c x}} (1 + c x) \right) \right] \\
 & \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 4 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
 & \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{1}{2} \left((1 + i) - (1 - i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right]
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i) + (1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - 4i\operatorname{ArcCosh}[cx] \\
 & \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + \\
 & 4i\operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + \\
 & 2\left(\operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \right. \\
 & \left. \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]\right) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & 2\left(\operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \right. \\
 & \left. \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]\right) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[cx]}\right] + \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, -i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 2\operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 2\operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 2\operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 2\operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 2\operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \operatorname{PolyLog}\left[2, -c x - \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right] + \\
 & 4 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \operatorname{PolyLog}\left[2, -c x - \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right] + \\
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \operatorname{PolyLog}\left[2, -i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] - \\
 & 4 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \operatorname{PolyLog}\left[2, i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] + \\
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \\
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \operatorname{PolyLog}\left[2, \right. \\
 & \quad \left. \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - 4 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right] \\
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 4 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 4 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - 2 \operatorname{PolyLog} \left[3, -i e^{-\operatorname{ArcCosh}[cx]} \right] + \\
 & 2 \operatorname{PolyLog} \left[3, i e^{-\operatorname{ArcCosh}[cx]} \right] - 4 \operatorname{PolyLog} \left[3, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] +
 \end{aligned}$$

$$4 \operatorname{PolyLog}\left[3, i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right)\right]$$

Problem 178: Result more than twice size of optimal antiderivative.

$$\int \frac{(d - c^2 d x^2)^{3/2} (a + b \operatorname{ArcCosh}[c x])^2}{x^3} dx$$

Optimal (type 4, 642 leaves, 18 steps):

$$\begin{aligned} & -2 b^2 c^2 d \sqrt{d - c^2 d x^2} + \frac{3 a b c^3 d x \sqrt{d - c^2 d x^2}}{\sqrt{-1+c x} \sqrt{1+c x}} + \frac{3 b^2 c^3 d x \sqrt{d - c^2 d x^2} \operatorname{ArcCosh}[c x]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\ & \frac{b c d \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])}{x \sqrt{-1+c x} \sqrt{1+c x}} - \frac{b c^3 d x \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])}{\sqrt{-1+c x} \sqrt{1+c x}} - \\ & \frac{3}{2} c^2 d \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])^2 - \frac{d (1 - c x) (1 + c x) \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])^2}{2 x^2} + \\ & \frac{3 c^2 d \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\ & \frac{b^2 c^2 d \sqrt{d - c^2 d x^2} \operatorname{ArcTan}\left[\sqrt{-1+c x} \sqrt{1+c x}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\ & \left(3 i b c^2 d \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right] \right) / \left(\sqrt{-1+c x} \sqrt{1+c x} \right) + \\ & \frac{3 i b c^2 d \sqrt{d - c^2 d x^2} (a + b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\ & \frac{3 i b^2 c^2 d \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\ & \frac{3 i b^2 c^2 d \sqrt{d - c^2 d x^2} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} \end{aligned}$$

Result (type 4, 5484 leaves):

$$\begin{aligned} & \left(-a^2 c^2 d - \frac{a^2 d}{2 x^2} \right) \sqrt{-d (-1 + c^2 x^2)} - \frac{3}{2} a^2 c^2 d^{3/2} \operatorname{Log}[x] + \frac{3}{2} a^2 c^2 d^{3/2} \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d (-1 + c^2 x^2)} \right] - \\ & 2 a b c^2 d \sqrt{-d (-1 + c x) (1 + c x)} \left(- \frac{c x}{\sqrt{\frac{-1+c x}{1+c x}} (1 + c x)} + \operatorname{ArcCosh}[c x] + \right. \end{aligned}$$

$$\begin{aligned}
 & \frac{i \operatorname{ArcCosh}[c x] \left(\operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] - \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] \right)}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} + \\
 & \left. \frac{i \left(\operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] \right)}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} \right) + \\
 & \left(i a b c^2 d^2 \left(-\frac{i \sqrt{\frac{-1+c x}{1+c x}} (1+c x)}{c x} - \frac{i (-1+c x) (1+c x) \operatorname{ArcCosh}[c x]}{c^2 x^2} + \right. \right. \\
 & \left. \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] - \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right. \\
 & \left. \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - \right. \\
 & \left. \left. \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] \right) \right) / \left(\sqrt{-d (-1+c x) (1+c x)} \right) - \\
 & b^2 c^2 d \sqrt{-d (-1+c x) (1+c x)} \left(2 - \frac{2 c x \operatorname{ArcCosh}[c x]}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} + \operatorname{ArcCosh}[c x]^2 + \right. \\
 & \left. (i (\operatorname{ArcCosh}[c x]^2 \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] - \operatorname{ArcCosh}[c x]^2 \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] + 2 \operatorname{ArcCosh}[c x] \right. \\
 & \left. \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - 2 \operatorname{ArcCosh}[c x] \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] + 2 \right. \\
 & \left. \left. \operatorname{PolyLog}\left[3, -i e^{-\operatorname{ArcCosh}[c x]}\right] - 2 \operatorname{PolyLog}\left[3, i e^{-\operatorname{ArcCosh}[c x]}\right] \right) \right) / \left(\sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & b^2 c^2 d \left(\frac{d \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \left(2 + \frac{\sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx]}{cx} \right)}{2cx \sqrt{-d(-1+cx)} (1+cx)} \right) + \\
 & \frac{1}{2\sqrt{-d(-1+cx)} (1+cx)} i d \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \left(4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] + \right. \\
 & \quad \operatorname{ArcCosh}[cx]^2 \operatorname{Log} \left[1 - i e^{-\operatorname{ArcCosh}[cx]} \right] - \operatorname{ArcCosh}[cx]^2 \operatorname{Log} \left[1 + i e^{-\operatorname{ArcCosh}[cx]} \right] - \\
 & \quad 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]} \right] + \\
 & \quad 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 + i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]} \right] \left. \right) + \\
 & \quad 2 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{1}{1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \\
 & \quad 2 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[-\frac{2}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \\
 & \quad 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \quad \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] + 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \quad \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 - 2 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \\
 & \quad \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \quad \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & \quad 2 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & \quad 2 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{(1-i) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] + \\
 & \quad 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \quad \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - 4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\frac{(1-i)\left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] + \\
 & 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\frac{(1-i)\left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] + \\
 & 2 \operatorname{Log}\left[i\left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right]^2 \operatorname{Log}\left[(1-i)\left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[i\left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right]^2 \operatorname{Log}\left[\frac{(1+i)\left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 4 \operatorname{Log}\left[-i\left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \operatorname{Log}\left[\frac{1}{2}\left((1+i) - (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & 4 \operatorname{Log}\left[\frac{1}{2}\left((1+i) - (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + 4 \operatorname{Log}\left[-i\left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 4 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[\frac{1}{2}\left((1+i) - (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right]^2 - 2 \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right]^2 + \\
 & 4 \operatorname{Log}\left[i\left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right)\left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + 4 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right)\left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - 2
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right]-2\operatorname{Log}\left[\left(-\frac{1}{2}-\frac{i}{2}\right)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right]- \\
 & 2\operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
 & 2\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]^2\operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
 & 2\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
 & 4\operatorname{Log}\left[i\left[cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right]\right]\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
 & 4\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
 & 2\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]^2 \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+2\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
 & 2\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]-4i\operatorname{ArcCosh}[cx] \\
 & \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]+ \\
 & 2\operatorname{ArcCosh}[cx]\operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right]\operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]- \\
 & 2\operatorname{ArcCosh}[cx]\operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right]\operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]+
 \end{aligned}$$

$$\begin{aligned}
 & 4 \operatorname{ArcCosh}[c x] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] - \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] + \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] + \\
 & 2 \left(\operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] \right) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - \\
 & 2 \left(\operatorname{Log}\left[1 - \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+cx)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2cx}\right] \right) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] + \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] + \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] + \\
 & 2 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -c x - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
 & 4 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -c x - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -i \left(c x + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 4 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] + 4 \operatorname{Log} \left[\right. \\
 & \quad \left. -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \operatorname{PolyLog} \left[2, \right. \\
 & \quad \left. \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - 4 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 4 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] -
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 2 \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 2 \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 4 \operatorname{Log}\left[i\left(c x+\sqrt{\frac{-1+c x}{1+c x}}(1+c x)\right)\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 2 \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 2 \operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]- \\
 & 2 \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]- \\
 & 2 \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]-2 \operatorname{PolyLog}\left[3,-i e^{-\operatorname{ArcCosh}[c x]}\right]+ \\
 & 2 \operatorname{PolyLog}\left[3,i e^{-\operatorname{ArcCosh}[c x]}\right]-4 \operatorname{PolyLog}\left[3,-i\left(c x+\sqrt{\frac{-1+c x}{1+c x}}(1+c x)\right)\right]+ \\
 & \left. 4 \operatorname{PolyLog}\left[3,i\left(c x+\sqrt{\frac{-1+c x}{1+c x}}(1+c x)\right)\right]\right)
 \end{aligned}$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{(d-c^2 d x^2)^{5/2} (a+b \operatorname{ArcCosh}[c x])^2}{x^3} dx$$

Optimal (type 4, 921 leaves, 27 steps):

$$\begin{aligned}
 & -\frac{170}{27} b^2 c^2 d^2 \sqrt{d-c^2 d x^2} + \frac{5}{27} b^2 c^4 d^2 x^2 \sqrt{d-c^2 d x^2} + \\
 & \frac{5 a b c^3 d^2 x \sqrt{d-c^2 d x^2}}{\sqrt{-1+c x} \sqrt{1+c x}} + \frac{5 b^2 c^2 d^2 (1-c^2 x^2) \sqrt{d-c^2 d x^2}}{3 (1-c x) (1+c x)} + \\
 & \frac{b^2 c^2 d^2 (1-c^2 x^2)^2 \sqrt{d-c^2 d x^2}}{9 (1-c x) (1+c x)} + \frac{5 b^2 c^3 d^2 x \sqrt{d-c^2 d x^2} \operatorname{ArcCosh}[c x]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\
 & \frac{b c d^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{x \sqrt{-1+c x} \sqrt{1+c x}} - \frac{b c^3 d^2 x \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{3 \sqrt{-1+c x} \sqrt{1+c x}} - \\
 & \frac{2 b c^5 d^2 x^3 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])}{9 \sqrt{-1+c x} \sqrt{1+c x}} - \frac{5}{2} c^2 d^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2 - \\
 & \frac{5}{6} c^2 d^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2 - \\
 & \frac{d^2 (1-c x)^2 (1+c x)^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2}{2 x^2} + \\
 & \frac{5 c^2 d^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\
 & \frac{b^2 c^2 d^2 \sqrt{-1+c^2 x^2} \sqrt{d-c^2 d x^2} \operatorname{ArcTan}\left[\sqrt{-1+c^2 x^2}\right]}{(1-c x) (1+c x)} - \\
 & \left(\frac{5 i b c^2 d^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} \right) / \left(\sqrt{-1+c x} \sqrt{1+c x} \right) + \\
 & \frac{5 i b c^2 d^2 \sqrt{d-c^2 d x^2} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} + \\
 & \frac{5 i b^2 c^2 d^2 \sqrt{d-c^2 d x^2} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}} - \\
 & \frac{5 i b^2 c^2 d^2 \sqrt{d-c^2 d x^2} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{-1+c x} \sqrt{1+c x}}
 \end{aligned}$$

Result (type 4, 5734 leaves):

$$\begin{aligned}
 & \sqrt{-d (-1+c^2 x^2)} \left(-\frac{7}{3} a^2 c^2 d^2 - \frac{a^2 d^2}{2 x^2} + \frac{1}{3} a^2 c^4 d^2 x^2 \right) - \left(a b c^2 d^2 \sqrt{-d (-1+c x) (1+c x)} \right. \\
 & \left. \left(-9 c x - 12 \left(\frac{-1+c x}{1+c x} \right)^{3/2} (1+c x)^3 \operatorname{ArcCosh}[c x] + \operatorname{Cosh}\left[3 \operatorname{ArcCosh}[c x]\right] \right) \right) / \\
 & \left(18 \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) + \frac{1}{54} b^2 c^2 d^2 \sqrt{-d (-1+c x) (1+c x)}
 \end{aligned}$$

$$\left(-26 + \frac{27 c x \operatorname{ArcCosh}[c x]}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} - 9 \operatorname{ArcCosh}[c x]^2 + \right.$$

$$\left. (2 + 9 \operatorname{ArcCosh}[c x]^2) \operatorname{Cosh}[2 \operatorname{ArcCosh}[c x]] - \frac{3 \operatorname{ArcCosh}[c x] \operatorname{Cosh}[3 \operatorname{ArcCosh}[c x]]}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} \right) -$$

$$\frac{5}{2} a^2 c^2 d^{5/2} \operatorname{Log}[x] + \frac{5}{2} a^2 c^2 d^{5/2} \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d(-1+c^2 x^2)}\right] -$$

$$4 a b c^2 d^2 \sqrt{-d(-1+c x)(1+c x)} \left(-\frac{c x}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} + \operatorname{ArcCosh}[c x] + \right.$$

$$\left. \frac{i \operatorname{ArcCosh}[c x] (\operatorname{Log}[1 - i e^{-\operatorname{ArcCosh}[c x]}] - \operatorname{Log}[1 + i e^{-\operatorname{ArcCosh}[c x]}])}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} + \right.$$

$$\left. \frac{i (\operatorname{PolyLog}[2, -i e^{-\operatorname{ArcCosh}[c x]}] - \operatorname{PolyLog}[2, i e^{-\operatorname{ArcCosh}[c x]}])}{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)} \right) +$$

$$\left(i a b c^2 d^3 \left(-\frac{i \sqrt{\frac{-1+c x}{1+c x}} (1+c x)}{c x} - \frac{i (-1+c x)(1+c x) \operatorname{ArcCosh}[c x]}{c^2 x^2} + \right. \right.$$

$$\left. \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x] \operatorname{Log}[1 - i e^{-\operatorname{ArcCosh}[c x]}] - \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right.$$

$$\left. \operatorname{ArcCosh}[c x] \operatorname{Log}[1 + i e^{-\operatorname{ArcCosh}[c x]}] + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}[2, -i e^{-\operatorname{ArcCosh}[c x]}] - \right.$$

$$\left. \left. \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}[2, i e^{-\operatorname{ArcCosh}[c x]}] \right) \right) / \left(\sqrt{-d(-1+c x)(1+c x)} \right) -$$

$$\begin{aligned}
 & 2 b^2 c^2 d^2 \sqrt{-d(-1+cx)(1+cx)} \left(2 - \frac{2cx \operatorname{ArcCosh}[cx]}{\sqrt{\frac{-1+cx}{1+cx}}(1+cx)} + \operatorname{ArcCosh}[cx]^2 + \right. \\
 & \left. (\operatorname{ArcCosh}[cx]^2 \operatorname{Log}[1 - i e^{-\operatorname{ArcCosh}[cx]}] - \operatorname{ArcCosh}[cx]^2 \operatorname{Log}[1 + i e^{-\operatorname{ArcCosh}[cx]}] + 2 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}[2, -i e^{-\operatorname{ArcCosh}[cx]}] - 2 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}[2, i e^{-\operatorname{ArcCosh}[cx]}] + 2 \right. \\
 & \left. \operatorname{PolyLog}[3, -i e^{-\operatorname{ArcCosh}[cx]}] - 2 \operatorname{PolyLog}[3, i e^{-\operatorname{ArcCosh}[cx]}]) \right) / \left(\sqrt{\frac{-1+cx}{1+cx}}(1+cx) \right) + \\
 & b^2 c^2 d^2 \left(\frac{d \sqrt{\frac{-1+cx}{1+cx}}(1+cx) \operatorname{ArcCosh}[cx] \left(2 + \frac{\sqrt{\frac{-1+cx}{1+cx}}(1+cx) \operatorname{ArcCosh}[cx]}{cx} \right)}{2cx \sqrt{-d(-1+cx)(1+cx)}} + \right. \\
 & \frac{1}{2 \sqrt{-d(-1+cx)(1+cx)}} i d \sqrt{\frac{-1+cx}{1+cx}}(1+cx) \left(4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + \right. \\
 & \operatorname{ArcCosh}[cx]^2 \operatorname{Log}[1 - i e^{-\operatorname{ArcCosh}[cx]}] - \operatorname{ArcCosh}[cx]^2 \operatorname{Log}[1 + i e^{-\operatorname{ArcCosh}[cx]}] - \\
 & 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1 - i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 4 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1 + i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 2 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx) \right) \right]^2 \operatorname{Log}\left[\frac{1}{1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx) \right) \right]^2 \operatorname{Log}\left[-\frac{2}{-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]^2 - 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}}(1+cx) \right) \right]^2 \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]^2 \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right]^2 \operatorname{Log}\left[\frac{(1-i) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] + \\
 & 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] - 4 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] + \\
 & 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] + \\
 & 2 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right]^2 \operatorname{Log}\left[(1-i) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right]^2 \operatorname{Log}\left[\frac{(1+i) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] - \\
 & 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \operatorname{Log}\left[\frac{1}{2} \left(\left(1+i\right) - \left(1-i\right) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 4 \operatorname{Log}\left[\frac{1}{2} \left(\left(1+i\right) - \left(1-i\right) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + 4 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 4 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\frac{(1+i)\left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i) + (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - 4 i \operatorname{ArcCosh}[c x] \\
 & \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[1 - \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] + \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 - \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] - \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 - \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] + \\
 & 4 i \operatorname{ArcCosh}[c x] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[1 + \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] - \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 + \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] + \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1 + \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] + \\
 & 2 \left(\operatorname{Log}\left[1 - \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] \right) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - \\
 & 2 \left(\operatorname{Log}\left[1 - \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+c x)\left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right] \right) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] + \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{PolyLog}\left[2, -i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] + \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{ArcCosh}[c x] \operatorname{PolyLog}\left[2, i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] - \\
 & 2 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, i e^{2 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right]}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{PolyLog} \left[2, i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]} \right] - \\
 & 4 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{PolyLog} \left[2, -c x - \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right] + \\
 & 4 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{PolyLog} \left[2, -c x - \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right] + \\
 & 4 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{PolyLog} \left[2, -i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] - \\
 & 4 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{PolyLog} \left[2, i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] + 4 \operatorname{Log} \left[\right. \\
 & \quad \left. -i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] \operatorname{PolyLog} \left[2, \right. \\
 & \quad \left. \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - 4 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]\right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 4 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 4 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 2 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
 & \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - 2 \operatorname{PolyLog} \left[3, -i e^{-\operatorname{ArcCosh}[cx]} \right] + \\
 & 2 \operatorname{PolyLog} \left[3, i e^{-\operatorname{ArcCosh}[cx]} \right] - 4 \operatorname{PolyLog} \left[3, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] +
 \end{aligned}$$

$$4 \operatorname{PolyLog}\left[3, i \left(c x + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]$$

Problem 196: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcCosh}[cx])^2}{\sqrt{d - c^2 dx^2}} dx$$

Optimal (type 3, 53 leaves, 2 steps):

$$\frac{\sqrt{-1+cx} \sqrt{1+cx} (a + b \operatorname{ArcCosh}[cx])^3}{3bc \sqrt{d - c^2 dx^2}}$$

Result (type 3, 147 leaves):

$$\frac{1}{3c} \left(\frac{3ab \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx]^2}{\sqrt{d - c^2 dx^2}} + \frac{b^2 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx]^3}{\sqrt{d - c^2 dx^2}} - \frac{3a^2 \operatorname{ArcTan}\left[\frac{cx \sqrt{d - c^2 dx^2}}{\sqrt{d} (-1 + c^2 x^2)}\right]}{\sqrt{d}} \right)$$

Problem 199: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + b \operatorname{ArcCosh}[cx])^2}{x^3 \sqrt{d - c^2 dx^2}} dx$$

Optimal (type 4, 438 leaves, 13 steps):

$$\begin{aligned}
 & \frac{b c \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])}{x \sqrt{d-c^2 d x^2}} - \frac{(1-c x)(1+c x)(a+b \operatorname{ArcCosh}[c x])^2}{2 x^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{d-c^2 d x^2}} - \\
 & \frac{b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{ArcTan}\left[\sqrt{-1+c x} \sqrt{1+c x}\right]}{\sqrt{d-c^2 d x^2}} - \frac{1}{\sqrt{d-c^2 d x^2}} \\
 & \frac{i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{d-c^2 d x^2}} + \\
 & \frac{1}{\sqrt{d-c^2 d x^2}} i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right] + \\
 & \frac{i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{d-c^2 d x^2}} - \\
 & \frac{i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{\sqrt{d-c^2 d x^2}}
 \end{aligned}$$

Result (type 4, 5161 leaves):

$$\begin{aligned}
 & -\frac{a^2 \sqrt{-d(-1+c^2 x^2)}}{2 d x^2} + \frac{a^2 c^2 \operatorname{Log}[x]}{2 \sqrt{d}} - \frac{a^2 c^2 \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d(-1+c^2 x^2)}\right]}{2 \sqrt{d}} + \\
 & \left(a b c^2 \left(\frac{\sqrt{\frac{-1+c x}{1+c x}} (1+c x)}{c x} + \frac{(-1+c x)(1+c x) \operatorname{ArcCosh}[c x]}{c^2 x^2} - \right. \right. \\
 & \quad \left. \left. i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[c x]}\right] + i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right. \right. \\
 & \quad \left. \left. \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[c x]}\right] - i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] + \right. \right. \\
 & \quad \left. \left. i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] \right) \right) / \left(\sqrt{-d(-1+c x)(1+c x)} \right) + \\
 & b^2 c^2 \left(\frac{\sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x] \left(2 + \frac{\sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x]}{c x} \right)}{2 c x \sqrt{-d(-1+c x)(1+c x)}} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2} \left(\left(2 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) (-2 + \operatorname{ArcCosh}[cx])^2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \right) / \right. \\
 & \left(\sqrt{-d(-1+cx)(1+cx)} \right) - \left(2 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \right. \\
 & \left. \left(2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \left(\operatorname{Log}\left[1 - i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \operatorname{Log}\left[1 + \right. \right. \right. \\
 & \left. \left. \left. i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] \right) + i \left(\operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] \right) \right) - \right. \\
 & \left. \left. \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] \right) \right) / \left(\sqrt{-d(-1+cx)(1+cx)} \right) + \\
 & 2 \left(\frac{1}{2 \sqrt{-d(-1+cx)(1+cx)}} \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \left(-2 \operatorname{ArcCosh}[cx]^2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcCosh}[cx]\right] \right] - i \operatorname{ArcCosh}[cx]^2 \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[cx]}\right] + i \operatorname{ArcCosh}[cx]^2 \right. \\
 & \left. \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] - 4 \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \right) \\
 & \left. \operatorname{Log}\left[1 - \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] - 2i \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 - \right. \right. \right. \\
 & \left. \left. \left. i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 - \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] + 2i \operatorname{ArcCosh}[\right. \right. \\
 & \left. \left. cx \right] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 - \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] \right) + \\
 & 4 \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\right. \\
 & \left. 1 + \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] + 2i \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 - \right. \\
 & \left. \left. i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] - 2i \operatorname{ArcCosh}[\right. \\
 & \left. \left. cx \right] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] \right) - \\
 & 2i \left(\operatorname{Log}\left[1 - \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] - \operatorname{Log}\left[\right. \right. \\
 & \left. \left. 1 + \frac{i(1+cx)(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right])^2}{2cx}\right] \right) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[cx]}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2i \left(\operatorname{Log} \left[1 - \frac{i(1+cx) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)^2}{2cx} \right] - \operatorname{Log} \left[\right. \right. \\
 & \quad \left. \left. 1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)^2}{2cx} \right] \right) \operatorname{PolyLog} \left[2, i e^{-\operatorname{ArcCosh}[cx]} \right] + \\
 & \quad \left. 2i \operatorname{PolyLog} \left[3, -i e^{-\operatorname{ArcCosh}[cx]} \right] - 2i \operatorname{PolyLog} \left[3, i e^{-\operatorname{ArcCosh}[cx]} \right] \right) - \\
 & \frac{1}{\sqrt{-d(-1+cx)}(1+cx)} i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \\
 & \left(\operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{1}{1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[-\frac{2}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \right. \\
 & \quad 2i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. -1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] + 2i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \quad \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 - \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\right. \\
 & \quad \left. \left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. -1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & \quad \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & \quad \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{(1-i) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] + \\
 & \quad 2i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. \frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - 2i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. -1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] +
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] + \\
 & \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right]^2 \operatorname{Log}\left[(1-i) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right]^2 \operatorname{Log}\left[\frac{(1+i) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] - \\
 & 2 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \operatorname{Log}\left[\frac{1}{2} \left((1+i) - \right.\right. \\
 & \quad \left.\left.(1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 2 \operatorname{Log}\left[\frac{1}{2} \left((1+i) - (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[-1 + \right. \\
 & \quad \left.\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \right.\right. \\
 & \quad \left.\left.\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \operatorname{Log}\left[\frac{1}{2} \left((1+i) - (1-i) \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]^2 - \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \right. \\
 & \quad \left. \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]^2 + \\
 & 2 \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 2 \operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \\
 & \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \operatorname{Log}\left[\left(-\frac{1}{2} - \frac{i}{2}\right) \right. \\
 & \quad \left. \left(i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right]^2 +
 \end{aligned}$$

$$\begin{aligned}
 & \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - \\
 & \operatorname{Log} \left[\left(-\frac{1}{2} - \frac{i}{2} \right) \left(i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
 & \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - \\
 & \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. \frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]^2 \\
 & \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] \\
 & \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
 & \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
 & 2 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
 & \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right]^2 \operatorname{Log} \left[\frac{1}{2} \left((1+i) + \right. \right. \\
 & \quad \left. \left. (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\right. \\
 & \quad \left. 1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] \\
 & \operatorname{Log} \left[\frac{1}{2} \left((1+i) + (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
 & \left(\operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] - \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \right) \operatorname{PolyLog} \left[\right. \\
 & \quad \left. 2, -i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]} \right] + \left(-\operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] + \right. \\
 & \quad \left. \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \right) \operatorname{PolyLog} \left[2, i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]} \right] -
 \end{aligned}$$

$$\begin{aligned}
& 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
& 2 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + 2 \\
& \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[2, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] - \\
& 2 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[2, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] + \\
& 2 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[2, \right. \\
& \quad \left. \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
& \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2, \right. \\
& \quad \left. \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
& \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \right. \\
& \quad \left. \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - 2 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right] \operatorname{PolyLog}\left[\right. \\
& \quad \left. 2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
& \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2, \right. \\
& \quad \left. \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] +
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2,\left(-\frac{1}{2}+\frac{i}{2}\right)\right. \\
 & \quad \left.(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right])\right] - 2 \operatorname{Log}\left[-i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & \operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] + 2 \operatorname{Log}\left[i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \\
 & \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & \operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2,\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] - 2 \operatorname{PolyLog}\left[3,-i\right]
 \end{aligned}$$

$$\left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) + 2 \operatorname{PolyLog}\left[3, i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \right)$$

Problem 209: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \operatorname{ArcCosh}[c x])^2}{x^3 (d-c^2 d x^2)^{3/2}} dx$$

Optimal (type 4, 650 leaves, 26 steps):

$$\begin{aligned} & \frac{b c \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])}{d x \sqrt{d-c^2 d x^2}} + \frac{3 c^2 (a+b \operatorname{ArcCosh}[c x])^2}{2 d \sqrt{d-c^2 d x^2}} - \\ & \frac{(a+b \operatorname{ArcCosh}[c x])^2}{2 d x^2 \sqrt{d-c^2 d x^2}} + \frac{3 c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} - \\ & \frac{b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{ArcTan}\left[\sqrt{-1+c x} \sqrt{1+c x}\right]}{d \sqrt{d-c^2 d x^2}} + \\ & \frac{4 b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{ArcTanh}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} + \\ & \frac{2 b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[2, -e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} - \frac{1}{d \sqrt{d-c^2 d x^2}} \\ & \frac{3 i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} + \\ & \frac{1}{d \sqrt{d-c^2 d x^2}} - \frac{3 i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} - \\ & \frac{2 b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[2, e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} + \\ & \frac{3 i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} - \\ & \frac{3 i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{d \sqrt{d-c^2 d x^2}} \end{aligned}$$

Result (type 4, 5400 leaves):

$$\begin{aligned} & \sqrt{-d(-1+c^2 x^2)} \left(-\frac{a^2}{2 d^2 x^2} - \frac{a^2 c^2}{d^2 (-1+c^2 x^2)} \right) + \\ & \frac{3 a^2 c^2 \operatorname{Log}[x]}{2 d^{3/2}} - \frac{3 a^2 c^2 \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d(-1+c^2 x^2)}\right]}{2 d^{3/2}} \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{d} b^2 c^2 \left(\frac{1}{2 \sqrt{-d(-1+cx)(1+cx)}} i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \left(-4 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \right) + \right. \\
 & 3 \operatorname{ArcCosh}[cx]^2 \operatorname{Log} \left[1 - i e^{-\operatorname{ArcCosh}[cx]} \right] - 3 \operatorname{ArcCosh}[cx]^2 \operatorname{Log} \left[1 + i e^{-\operatorname{ArcCosh}[cx]} \right] - \\
 & 12 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]} \right] + \\
 & 12 i \operatorname{ArcCosh}[cx] \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 + i e^{2 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]} \right] + \\
 & 6 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{1}{1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \\
 & 6 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[-\frac{2}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - \\
 & 12 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] + 12 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 - 6 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \\
 & \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + 6 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] - \\
 & 6 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right]^2 \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right] + \\
 & 6 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right]^2 \operatorname{Log} \left[\frac{(1-i) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] + \\
 & 12 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] - 12 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \\
 & \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] + \\
 & 6 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] \right) \right]
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right]+ \\
& 6 \operatorname{Log}\left[i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right]^2 \operatorname{Log}\left[(1-i)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 6 \operatorname{Log}\left[i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right]^2 \operatorname{Log}\left[\frac{(1+i)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right]- \\
& 12 \operatorname{Log}\left[-i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \operatorname{Log}\left[\frac{1}{2}\left((1+i)-(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 12 \operatorname{Log}\left[\frac{1}{2}\left((1+i)-(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 12 \operatorname{Log}\left[-i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+12 \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 6 \operatorname{Log}\left[\frac{1}{2}\left((1+i)-(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]^2-6 \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}-\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]^2+ \\
& 12 \operatorname{Log}\left[i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right] \operatorname{Log}\left[\left(-\frac{1}{2}-\frac{i}{2}\right)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 12 \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[\left(-\frac{1}{2}-\frac{i}{2}\right)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]-6 \operatorname{Log}\left[\left(-\frac{1}{2}-\frac{i}{2}\right)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\left(-\frac{1}{2}-\frac{i}{2}\right)\left(i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]^2+ \\
& 12 i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]
\end{aligned}$$

$$\begin{aligned}
& \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right]-6\operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 6\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]^2\operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 6\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{(1-i)\left(-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \\
& \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 12\operatorname{Log}\left[i\left(cx+\sqrt{\frac{-1+cx}{1+cx}}(1+cx)\right)\right]\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 12\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right] \\
& \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 6\operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]^2 \\
& \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+6\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]+ \\
& 6\operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]\operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]}\right] \\
& \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)\right]- \\
& 12i\operatorname{ArcCosh}[cx]\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right] \\
& \operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]+6\operatorname{ArcCosh}[cx] \\
& \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right]\operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]-6 \\
& \operatorname{ArcCosh}[cx]\operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right]\operatorname{Log}\left[1-\frac{i(1+cx)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right]+ \\
& 12i\operatorname{ArcCosh}[cx]\operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[cx]\right]\right]
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - 6 \operatorname{ArcCosh}[cx] \\
 & \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + 6 \\
 & \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] \operatorname{Log}\left[1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] + \\
 & 6 \left(\operatorname{Log}\left[1 - \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] \right) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & 6 \left(\operatorname{Log}\left[1 - \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[1 + \frac{i(1+cx) \left(-i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)^2}{2cx}\right] \right) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[cx]}\right] + \\
 & 6 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 6 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 6 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 6 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 6 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 6 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
 & 12 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
 & 12 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
 & 12 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] - \\
 & 12 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] +
 \end{aligned}$$

$$\begin{aligned}
& 12 \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \\
& \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
& 6 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
& 6 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
& \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \operatorname{PolyLog} \left[2, \right. \\
& \quad \left. \left(-\frac{1}{2} - \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - 12 \operatorname{Log} \left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \\
& \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
& \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
& 6 \operatorname{Log} \left[1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] + \\
& 6 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right] \\
& \operatorname{PolyLog} \left[2, \left(-\frac{1}{2} + \frac{i}{2} \right) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - 12 \\
& \operatorname{Log} \left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right] \operatorname{PolyLog} \left[2, \left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right) \right] - \\
& 6 \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [cx] \right]} \right]
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 6 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 6 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 12 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 6 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
 & 6 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & 6 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
 & 6 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - 6 \operatorname{PolyLog}\left[3, -i e^{-\operatorname{ArcCosh}[cx]}\right] + \\
 & 6 \operatorname{PolyLog}\left[3, i e^{-\operatorname{ArcCosh}[cx]}\right] - 12 \operatorname{PolyLog}\left[3, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] + \\
 & 12 \operatorname{PolyLog}\left[3, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] + \\
 & \frac{1}{2\sqrt{-d(-1+cx)(1+cx)}} \left(4 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, -e^{-\operatorname{ArcCosh}[cx]}\right] - \right. \\
 & \left. 4 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, e^{-\operatorname{ArcCosh}[cx]}\right] - \right)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{ArcCosh}[cx] \left(\frac{2 \sqrt{\frac{-1+cx}{1+cx}} (1+cx)}{cx} + \frac{(-1+cx)(1+cx) \operatorname{ArcCosh}[cx]}{c^2 x^2} + 2 \operatorname{ArcCosh}[cx] \right. \\
 & \left. \operatorname{Cosh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 - 4 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{Log}\left[1 - e^{-\operatorname{ArcCosh}[cx]}\right] + 4 \sqrt{\frac{-1+cx}{1+cx}} \right. \\
 & \left. (1+cx) \operatorname{Log}\left[1 + e^{-\operatorname{ArcCosh}[cx]}\right] - 2 \operatorname{ArcCosh}[cx] \operatorname{Sinh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 \right) - \\
 & \frac{1}{d \sqrt{-d(-1+cx)(1+cx)}} a b c^2 \left(-\frac{\sqrt{\frac{-1+cx}{1+cx}} (1+cx)}{cx} - \right. \\
 & \left. \frac{(-1+cx)(1+cx) \operatorname{ArcCosh}[cx]}{c^2 x^2} - \right. \\
 & 2 \operatorname{ArcCosh}[cx] \\
 & \operatorname{Cosh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 + 3 \\
 & i \sqrt{\frac{-1+cx}{1+cx}} \\
 & (1+cx) \\
 & \operatorname{ArcCosh}[cx] \\
 & \operatorname{Log}\left[1 - i e^{-\operatorname{ArcCosh}[cx]}\right] - 3 \\
 & i \sqrt{\frac{-1+cx}{1+cx}} \\
 & (1+cx) \\
 & \operatorname{ArcCosh}[cx] \\
 & \operatorname{Log}\left[1 + i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & 2 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + \\
 & 2 \sqrt{\frac{-1+cx}{1+cx}} \\
 & (1+cx)
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] + \\
 & 3 i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[c x]}\right] - \\
 & 3 i \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \\
 & \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[c x]}\right] + \\
 & \left. \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \operatorname{ArcCosh}[c x] \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right] \right)
 \end{aligned}$$

Problem 219: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+b \operatorname{ArcCosh}[c x])^2}{x^3 (d-c^2 d x^2)^{5/2}} dx$$

Optimal (type 4, 826 leaves, 39 steps):

$$\begin{aligned}
 & - \frac{b^2 c^2}{3 d^2 \sqrt{d-c^2 d x^2}} + \frac{b c \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])}{d^2 x (1-c^2 x^2) \sqrt{d-c^2 d x^2}} - \\
 & \frac{2 b c^3 x \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])}{3 d^2 (1-c^2 x^2) \sqrt{d-c^2 d x^2}} + \frac{5 c^2 (a+b \operatorname{ArcCosh}[c x])^2}{2 d^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{5 c^2 (a+b \operatorname{ArcCosh}[c x])^2}{6 d^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} - \frac{(a+b \operatorname{ArcCosh}[c x])^2}{2 d^2 x^2 (1-c x) (1+c x) \sqrt{d-c^2 d x^2}} + \\
 & \frac{5 c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x])^2 \operatorname{ArcTan}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{d^2 \sqrt{d-c^2 d x^2}} - \\
 & \frac{b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{ArcTan}\left[\sqrt{-1+c x} \sqrt{1+c x}\right]}{d^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{26 b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{ArcTanh}\left[e^{\operatorname{ArcCosh}[c x]}\right]}{3 d^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{13 b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[2, -e^{\operatorname{ArcCosh}[c x]}\right]}{3 d^2 \sqrt{d-c^2 d x^2}} - \frac{1}{d^2 \sqrt{d-c^2 d x^2}} \\
 & \frac{5 i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, -i e^{\operatorname{ArcCosh}[c x]}\right]}{d^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{1}{d^2 \sqrt{d-c^2 d x^2}} \frac{5 i b c^2 \sqrt{-1+c x} \sqrt{1+c x} (a+b \operatorname{ArcCosh}[c x]) \operatorname{PolyLog}\left[2, i e^{\operatorname{ArcCosh}[c x]}\right]}{d^2 \sqrt{d-c^2 d x^2}} - \\
 & \frac{13 b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[2, e^{\operatorname{ArcCosh}[c x]}\right]}{3 d^2 \sqrt{d-c^2 d x^2}} + \\
 & \frac{5 i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, -i e^{\operatorname{ArcCosh}[c x]}\right]}{d^2 \sqrt{d-c^2 d x^2}} - \\
 & \frac{5 i b^2 c^2 \sqrt{-1+c x} \sqrt{1+c x} \operatorname{PolyLog}\left[3, i e^{\operatorname{ArcCosh}[c x]}\right]}{d^2 \sqrt{d-c^2 d x^2}}
 \end{aligned}$$

Result (type 4, 5568 leaves):

$$\begin{aligned}
 & \sqrt{-d(-1+c^2 x^2)} \left(-\frac{a^2}{2 d^3 x^2} + \frac{a^2 c^2}{3 d^3 (-1+c^2 x^2)^2} - \frac{2 a^2 c^2}{d^3 (-1+c^2 x^2)} \right) + \\
 & \frac{5 a^2 c^2 \operatorname{Log}[x]}{2 d^{5/2}} - \frac{5 a^2 c^2 \operatorname{Log}\left[d + \sqrt{d} \sqrt{-d(-1+c^2 x^2)}\right]}{2 d^{5/2}} + \\
 & \frac{1}{6 d^2 \sqrt{-d(-1+c x)(1+c x)}} a b c^2 \left(\frac{6 \sqrt{\frac{-1+c x}{1+c x}} (1+c x)}{c x} + \frac{6 (-1+c x)(1+c x) \operatorname{ArcCosh}[c x]}{c^2 x^2} \right) + \\
 & 26 \operatorname{ArcCosh}[c x] \operatorname{Cosh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]^2 - \operatorname{Coth}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right] -
 \end{aligned}$$

$$\begin{aligned}
 & \operatorname{ArcCosh}[cx] \operatorname{Coth}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 - 30i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \\
 & \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right] + 30i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right] + \\
 & 26 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] - 26 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \\
 & \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] - 30i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, -i e^{-\operatorname{ArcCosh}[cx]}\right] + \\
 & 30i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog}\left[2, i e^{-\operatorname{ArcCosh}[cx]}\right] - 26 \operatorname{ArcCosh}[cx] \operatorname{Sinh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 - \\
 & \left. \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right] - \operatorname{ArcCosh}[cx] \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2\right) + \frac{1}{d^2} \\
 & b^2 c^2 \left(-\frac{1}{2 \sqrt{-d} (-1+cx) (1+cx)} i \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \left(-4i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \right) + \right. \\
 & 5 \operatorname{ArcCosh}[cx]^2 \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[cx]}\right] - 5 \operatorname{ArcCosh}[cx]^2 \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[cx]}\right] - \\
 & 20i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1-i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 20i \operatorname{ArcCosh}[cx] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1+i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
 & 10 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right]^2 \operatorname{Log}\left[\frac{1}{1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 10 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right]^2 \operatorname{Log}\left[-\frac{2}{-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] - \\
 & 20i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{Log}\left[1-\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] + 20i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \\
 & \left. \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]^2 - 10 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + 10 \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
& \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
& 10 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right]^2 \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
& 10 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right]^2 \operatorname{Log} \left[\frac{(1-i) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
& 20 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[1 - \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
& \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - 20 i \operatorname{ArcTan} \left[\operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \\
& \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
& 10 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
& \operatorname{Log} \left[\frac{(1-i) \left(-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] + \\
& 10 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right]^2 \operatorname{Log} \left[(1-i) \left(i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
& 10 \operatorname{Log} \left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right]^2 \operatorname{Log} \left[\frac{(1+i) \left(i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right)}{-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right]} \right] - 20 \\
& \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{Log} \left[\frac{1}{2} \left((1+i) - (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
& \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] - \\
& 20 \operatorname{Log} \left[\frac{1}{2} \left((1+i) - (1-i) \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
& \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + \\
& 20 \operatorname{Log} \left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x) \right) \right] \operatorname{Log} \left[\left(\frac{1}{2} + \frac{i}{2} \right) \left(-i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] \\
& \operatorname{Log} \left[\left(\frac{1}{2} - \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right) \right] + 20 \operatorname{Log} \left[-1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh} [c x] \right] \right] \operatorname{Log} \left[
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 10 \operatorname{Log}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)\right]^2 \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)\right]+10 \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)\right]+ \\
 & 10 \operatorname{Log}\left[-1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[\frac{(1+i)\left(1+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)}{i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{Log}\left[\frac{1}{2}\left((1+i)+(1-i)\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)\right]-20 i \operatorname{ArcCosh}[c x] \\
 & \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right] \operatorname{Log}\left[1-\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]+ \\
 & 10 \operatorname{ArcCosh}[c x] \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[c x]}\right] \\
 & \operatorname{Log}\left[1-\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]-10 \operatorname{ArcCosh}[c x] \\
 & \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1-\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]+ \\
 & 20 i \operatorname{ArcCosh}[c x] \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right] \\
 & \operatorname{Log}\left[1+\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]-10 \operatorname{ArcCosh}[c x] \\
 & \operatorname{Log}\left[1-i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1+\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]+10 \operatorname{ArcCosh}[\\
 & c x] \operatorname{Log}\left[1+i e^{-\operatorname{ArcCosh}[c x]}\right] \operatorname{Log}\left[1+\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]+ \\
 & 10\left(\operatorname{Log}\left[1-\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]-\right. \\
 & \left.\operatorname{Log}\left[1+\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]\right) \operatorname{PolyLog}\left[2,-i e^{-\operatorname{ArcCosh}[c x]}\right]- \\
 & 10\left(\operatorname{Log}\left[1-\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]-\right. \\
 & \left.\operatorname{Log}\left[1+\frac{i(1+c x)\left(-i+\operatorname{Tanh}\left[\frac{1}{2}\operatorname{ArcCosh}[c x]\right]\right)^2}{2 c x}\right]\right) \operatorname{PolyLog}\left[2,i e^{-\operatorname{ArcCosh}[c x]}\right]+
 \end{aligned}$$

$$\begin{aligned}
& 10 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
& 10 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
& 10 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, -i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
& 10 \operatorname{ArcCosh}[cx] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
& 10 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] + \\
& 10 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, i e^{2i \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right]}\right] - \\
& 20 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
& 20 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -cx - \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right] + \\
& 20 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] - \\
& 20 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \operatorname{PolyLog}\left[2, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] + \\
& 20 \operatorname{Log}\left[-i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + 10 \\
& \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] + \\
& 10 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \\
& \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - 10 \\
& \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - \\
& 10 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]}\right] \operatorname{PolyLog}\left[2, \right. \\
& \left. \left(-\frac{1}{2} - \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]\right)\right] - 20 \operatorname{Log}\left[i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx)\right)\right]
\end{aligned}$$

$$\begin{aligned}
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - 10 \\
 & \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 10 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + 10 \\
 & \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 10 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \operatorname{PolyLog}\left[2, \right. \\
 & \quad \left. \left(-\frac{1}{2} + \frac{i}{2}\right) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - 20 \operatorname{Log}\left[-i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 10 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 10 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 10 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 10 \operatorname{Log}\left[\frac{(1+i) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} - \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + 20 \\
 & \operatorname{Log}\left[i \left(c x + \sqrt{\frac{-1+c x}{1+c x}} (1+c x)\right)\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 10 \operatorname{Log}\left[1 - \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] + \\
 & 10 \operatorname{Log}\left[\frac{(1-i) \left(-1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)}{i + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]}\right] \\
 & \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] - \\
 & 10 \operatorname{Log}\left[1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right] \operatorname{PolyLog}\left[2, \left(\frac{1}{2} + \frac{i}{2}\right) \left(1 + \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[c x]\right]\right)\right] -
 \end{aligned}$$

$$\begin{aligned}
& 10 \operatorname{Log} \left[\frac{(1+i) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]\right)}{i + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]} \right] \\
& \operatorname{PolyLog} \left[2, \left(\frac{1}{2} + \frac{i}{2} \right) \left(1 + \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]\right) \right] - 10 \operatorname{PolyLog} \left[3, -i e^{-\operatorname{ArcCosh}[cx]} \right] + \\
& 10 \operatorname{PolyLog} \left[3, i e^{-\operatorname{ArcCosh}[cx]} \right] - 20 \operatorname{PolyLog} \left[3, -i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] + \\
& 20 \operatorname{PolyLog} \left[3, i \left(cx + \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \right) \right] + \\
& \frac{1}{12 \sqrt{-d(-1+cx)(1+cx)}} \left(\frac{12 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx]}{cx} + \right. \\
& \frac{6(-1+cx)(1+cx) \operatorname{ArcCosh}[cx]^2}{c^2 x^2} - 4 \operatorname{Cosh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]^2 + \\
& 26 \operatorname{ArcCosh}[cx]^2 \operatorname{Cosh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]^2 - \\
& 2 \operatorname{ArcCosh}[cx] \operatorname{Coth} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] - \\
& \operatorname{ArcCosh}[cx]^2 \operatorname{Coth} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]^2 - \\
& 52 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \operatorname{Log} \left[1 - e^{-\operatorname{ArcCosh}[cx]} \right] + \\
& 52 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{ArcCosh}[cx] \operatorname{Log} \left[1 + e^{-\operatorname{ArcCosh}[cx]} \right] - \\
& 52 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog} \left[2, -e^{-\operatorname{ArcCosh}[cx]} \right] + \\
& 52 \sqrt{\frac{-1+cx}{1+cx}} (1+cx) \operatorname{PolyLog} \left[2, e^{-\operatorname{ArcCosh}[cx]} \right] + \\
& 4 \operatorname{Sinh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]^2 - 26 \operatorname{ArcCosh}[cx]^2 \operatorname{Sinh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right]^2 - \\
& 2 \operatorname{ArcCosh}[cx] \operatorname{Tanh} \left[\frac{1}{2} \operatorname{ArcCosh}[cx] \right] -
\end{aligned}$$

$$\left. \left. \operatorname{ArcCosh}[cx]^2 \operatorname{Tanh}\left[\frac{1}{2} \operatorname{ArcCosh}[cx]\right]^2 \right) \right)$$

Problem 250: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{ArcCosh}[ax]^3}{(c-a^2cx^2)^{3/2}} dx$$

Optimal (type 4, 241 leaves, 8 steps):

$$\begin{aligned} & \frac{x \operatorname{ArcCosh}[ax]^3}{c \sqrt{c-a^2cx^2}} + \frac{\sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[ax]^3}{a c \sqrt{c-a^2cx^2}} - \\ & \frac{3 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[ax]^2 \operatorname{Log}[1-e^{2 \operatorname{ArcCosh}[ax]}]}{a c \sqrt{c-a^2cx^2}} - \\ & \frac{3 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[ax] \operatorname{PolyLog}[2, e^{2 \operatorname{ArcCosh}[ax]}]}{a c \sqrt{c-a^2cx^2}} + \\ & \frac{3 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{PolyLog}[3, e^{2 \operatorname{ArcCosh}[ax]}]}{2 a c \sqrt{c-a^2cx^2}} \end{aligned}$$

Result (type 4, 212 leaves):

$$\begin{aligned} & - \left(\left(i \pi^3 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) - 8 a x \operatorname{ArcCosh}[ax]^3 - 8 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \operatorname{ArcCosh}[ax]^3 + \right. \right. \\ & \quad 24 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \operatorname{ArcCosh}[ax]^2 \operatorname{Log}[1-e^{2 \operatorname{ArcCosh}[ax]}] + \\ & \quad 24 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \operatorname{ArcCosh}[ax] \operatorname{PolyLog}[2, e^{2 \operatorname{ArcCosh}[ax]}] - \\ & \quad \left. \left. 12 \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \operatorname{PolyLog}[3, e^{2 \operatorname{ArcCosh}[ax]}] \right) / \left(8 a c \sqrt{-c(-1+ax)(1+ax)} \right) \right) \end{aligned}$$

Problem 251: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{ArcCosh}[ax]^3}{(c-a^2cx^2)^{5/2}} dx$$

Optimal (type 4, 428 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{x \operatorname{ArcCosh}[a x]}{c^2 \sqrt{c-a^2 c x^2}} + \frac{\sqrt{-1+a x} \sqrt{1+a x} \operatorname{ArcCosh}[a x]^2}{2 a c^2 (1-a^2 x^2) \sqrt{c-a^2 c x^2}} + \frac{2 x \operatorname{ArcCosh}[a x]^3}{3 c^2 \sqrt{c-a^2 c x^2}} + \\
 & \frac{x \operatorname{ArcCosh}[a x]^3}{3 c^2 (1-a x) (1+a x) \sqrt{c-a^2 c x^2}} + \frac{2 \sqrt{-1+a x} \sqrt{1+a x} \operatorname{ArcCosh}[a x]^3}{3 a c^2 \sqrt{c-a^2 c x^2}} - \\
 & \frac{2 \sqrt{-1+a x} \sqrt{1+a x} \operatorname{ArcCosh}[a x]^2 \operatorname{Log}\left[1-e^{2 \operatorname{ArcCosh}[a x]}\right]}{a c^2 \sqrt{c-a^2 c x^2}} + \frac{\sqrt{-1+a x} \sqrt{1+a x} \operatorname{Log}\left[1-a^2 x^2\right]}{2 a c^2 \sqrt{c-a^2 c x^2}} - \\
 & \frac{2 \sqrt{-1+a x} \sqrt{1+a x} \operatorname{ArcCosh}[a x] \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[a x]}\right]}{a c^2 \sqrt{c-a^2 c x^2}} + \\
 & \frac{\sqrt{-1+a x} \sqrt{1+a x} \operatorname{PolyLog}\left[3, e^{2 \operatorname{ArcCosh}[a x]}\right]}{a c^2 \sqrt{c-a^2 c x^2}}
 \end{aligned}$$

Result (type 4, 258 leaves):

$$\left(\sqrt{\frac{-1+a x}{1+a x}} (1+a x) \left(-i \pi^3 - \frac{12 a x \sqrt{\frac{-1+a x}{1+a x}} \operatorname{ArcCosh}[a x]}{-1+a x} + \frac{6 \operatorname{ArcCosh}[a x]^2}{1-a^2 x^2} + \right. \right.$$

$$\left. \left. 8 \operatorname{ArcCosh}[a x]^3 + \frac{8 a x \sqrt{\frac{-1+a x}{1+a x}} \operatorname{ArcCosh}[a x]^3}{-1+a x} - \frac{4 a x \left(\frac{-1+a x}{1+a x}\right)^{3/2} \operatorname{ArcCosh}[a x]^3}{(-1+a x)^3} - \right. \right.$$

$$\left. \left. 24 \operatorname{ArcCosh}[a x]^2 \operatorname{Log}\left[1-e^{2 \operatorname{ArcCosh}[a x]}\right] + 12 \operatorname{Log}\left[\sqrt{\frac{-1+a x}{1+a x}} (1+a x)\right] - 24 \operatorname{ArcCosh}[a x] \right. \right.$$

$$\left. \left. \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[a x]}\right] + 12 \operatorname{PolyLog}\left[3, e^{2 \operatorname{ArcCosh}[a x]}\right] \right) \right) / \left(12 a c^2 \sqrt{c-a^2 c x^2} \right)$$

Problem 252: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{ArcCosh}[a x]^3}{(c-a^2 c x^2)^{7/2}} dx$$

Optimal (type 4, 637 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{\sqrt{-1+ax} \sqrt{1+ax}}{20 a c^3 (1-a^2 x^2) \sqrt{c-a^2 c x^2}} - \frac{x \operatorname{ArcCosh}[a x]}{c^3 \sqrt{c-a^2 c x^2}} - \frac{x \operatorname{ArcCosh}[a x]}{10 c^3 (1-a x) (1+a x) \sqrt{c-a^2 c x^2}} + \\
 & \frac{3 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[a x]^2}{20 a c^3 (1-a^2 x^2)^2 \sqrt{c-a^2 c x^2}} + \frac{2 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[a x]^2}{5 a c^3 (1-a^2 x^2) \sqrt{c-a^2 c x^2}} + \frac{8 x \operatorname{ArcCosh}[a x]^3}{15 c^3 \sqrt{c-a^2 c x^2}} + \\
 & \frac{x \operatorname{ArcCosh}[a x]^3}{5 c^3 (1-a x)^2 (1+a x)^2 \sqrt{c-a^2 c x^2}} + \frac{4 x \operatorname{ArcCosh}[a x]^3}{15 c^3 (1-a x) (1+a x) \sqrt{c-a^2 c x^2}} + \\
 & \frac{8 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[a x]^3}{15 a c^3 \sqrt{c-a^2 c x^2}} - \frac{8 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[a x]^2 \operatorname{Log}\left[1 - e^{2 \operatorname{ArcCosh}[a x]}\right]}{5 a c^3 \sqrt{c-a^2 c x^2}} + \\
 & \frac{\sqrt{-1+ax} \sqrt{1+ax} \operatorname{Log}\left[1 - a^2 x^2\right]}{2 a c^3 \sqrt{c-a^2 c x^2}} - \frac{8 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{ArcCosh}[a x] \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[a x]}\right]}{5 a c^3 \sqrt{c-a^2 c x^2}} + \\
 & \frac{4 \sqrt{-1+ax} \sqrt{1+ax} \operatorname{PolyLog}\left[3, e^{2 \operatorname{ArcCosh}[a x]}\right]}{5 a c^3 \sqrt{c-a^2 c x^2}}
 \end{aligned}$$

Result (type 4, 363 leaves):

$$\begin{aligned}
 & - \frac{1}{60 a c^3 \sqrt{c-a^2 c x^2}} \sqrt{\frac{-1+ax}{1+ax}} (1+ax) \\
 & \left(4 i \pi^3 + \frac{3}{1-a^2 x^2} + \frac{60 a x \sqrt{\frac{-1+ax}{1+ax}} \operatorname{ArcCosh}[a x]}{-1+ax} - \frac{6 a x \left(\frac{-1+ax}{1+ax}\right)^{3/2} \operatorname{ArcCosh}[a x]}{(-1+ax)^3} - \right. \\
 & \frac{9 \operatorname{ArcCosh}[a x]^2}{(-1+a^2 x^2)^2} + \frac{24 \operatorname{ArcCosh}[a x]^2}{-1+a^2 x^2} - 32 \operatorname{ArcCosh}[a x]^3 - \frac{32 a x \sqrt{\frac{-1+ax}{1+ax}} \operatorname{ArcCosh}[a x]^3}{-1+ax} + \\
 & \frac{16 a x \left(\frac{-1+ax}{1+ax}\right)^{3/2} \operatorname{ArcCosh}[a x]^3}{(-1+ax)^3} - \frac{12 a x \sqrt{\frac{-1+ax}{1+ax}} \operatorname{ArcCosh}[a x]^3}{(-1+ax)^3 (1+ax)^2} + \\
 & \left. 96 \operatorname{ArcCosh}[a x]^2 \operatorname{Log}\left[1 - e^{2 \operatorname{ArcCosh}[a x]}\right] - 60 \operatorname{Log}\left[\sqrt{\frac{-1+ax}{1+ax}} (1+ax)\right] + \right. \\
 & \left. 96 \operatorname{ArcCosh}[a x] \operatorname{PolyLog}\left[2, e^{2 \operatorname{ArcCosh}[a x]}\right] - 48 \operatorname{PolyLog}\left[3, e^{2 \operatorname{ArcCosh}[a x]}\right] \right)
 \end{aligned}$$

Problem 336: Attempted integration timed out after 120 seconds.

$$\int \frac{\sqrt{1-c^2x^2}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 68 leaves, 1 step):

$$\frac{\sqrt{1-c^2x^2} \operatorname{Int}\left[\frac{\sqrt{-1+cx} \sqrt{1+cx}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2}, x\right]}{\sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 337: Attempted integration timed out after 120 seconds.

$$\int \frac{\sqrt{1-c^2x^2}}{x^4 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 68 leaves, 1 step):

$$\frac{\sqrt{1-c^2x^2} \operatorname{Int}\left[\frac{\sqrt{-1+cx} \sqrt{1+cx}}{x^4 (a+b \operatorname{ArcCosh}[cx])^2}, x\right]}{\sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 344: Attempted integration timed out after 120 seconds.

$$\int \frac{(1-c^2x^2)^{3/2}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 69 leaves, 1 step):

$$\frac{\sqrt{1-c^2x^2} \operatorname{Int}\left[\frac{(-1+cx)^{3/2} (1+cx)^{3/2}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2}, x\right]}{\sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 345: Attempted integration timed out after 120 seconds.

$$\int \frac{(1-c^2x^2)^{3/2}}{x^4 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 127 leaves, 2 steps):

$$\frac{(1-cx)^2 (1+cx)^{3/2} \sqrt{1-c^2 x^2}}{bcx^4 \sqrt{-1+cx} (a+b \operatorname{ArcCosh}[cx])} - \frac{4 \sqrt{1-c^2 x^2} \operatorname{Int}\left[\frac{-1+c^2 x^2}{x^5 (a+b \operatorname{ArcCosh}[cx])}, x\right]}{bc \sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 346: Attempted integration timed out after 120 seconds.

$$\int \frac{(1-c^2 x^2)^{3/2}}{x^5 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 69 leaves, 1 step):

$$\frac{\sqrt{1-c^2 x^2} \operatorname{Int}\left[\frac{(-1+cx)^{3/2} (1+cx)^{3/2}}{x^5 (a+b \operatorname{ArcCosh}[cx])^2}, x\right]}{\sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 352: Attempted integration timed out after 120 seconds.

$$\int \frac{(1-c^2 x^2)^{5/2}}{x^2 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 195 leaves, 2 steps):

$$\frac{(1-cx)^3 (1+cx)^{5/2} \sqrt{1-c^2 x^2}}{bcx^2 \sqrt{-1+cx} (a+b \operatorname{ArcCosh}[cx])} + \frac{2 \sqrt{1-c^2 x^2} \operatorname{Int}\left[\frac{(-1+c^2 x^2)^2}{x^3 (a+b \operatorname{ArcCosh}[cx])}, x\right]}{bc \sqrt{-1+cx} \sqrt{1+cx}} + \frac{4c \sqrt{1-c^2 x^2} \operatorname{Int}\left[\frac{(-1+c^2 x^2)^2}{x (a+b \operatorname{ArcCosh}[cx])}, x\right]}{b \sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 353: Attempted integration timed out after 120 seconds.

$$\int \frac{(1-c^2 x^2)^{5/2}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2} dx$$

Optimal (type 8, 68 leaves, 1 step):

$$\frac{\sqrt{1-c^2 x^2} \operatorname{Int}\left[\frac{(-1+cx)^{5/2} (1+cx)^{5/2}}{x^3 (a+b \operatorname{ArcCosh}[cx])^2}, x\right]}{\sqrt{-1+cx} \sqrt{1+cx}}$$

Result (type 1, 1 leaves):

???

Problem 354: Attempted integration timed out after 120 seconds.

$$\int \frac{(1 - c^2 x^2)^{5/2}}{x^4 (a + b \operatorname{ArcCosh}[c x])^2} dx$$

Optimal (type 8, 68 leaves, 1 step):

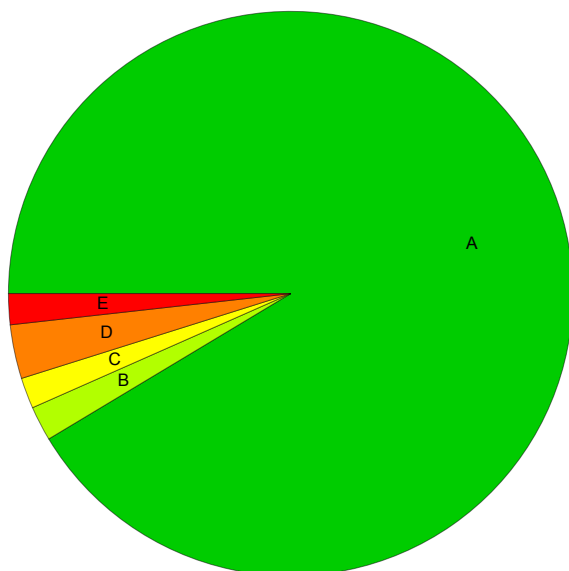
$$\frac{\sqrt{1 - c^2 x^2} \operatorname{Int}\left[\frac{(-1 + c x)^{5/2} (1 + c x)^{5/2}}{x^4 (a + b \operatorname{ArcCosh}[c x])^2}, x\right]}{\sqrt{-1 + c x} \sqrt{1 + c x}}$$

Result (type 1, 1 leaves):

???

Summary of Integration Test Results

453 integration problems



A - 414 optimal antiderivatives

B - 9 more than twice size of optimal antiderivatives

C - 8 unnecessarily complex antiderivatives

D - 14 unable to integrate problems

E - 8 integration timeouts